

Physics of Partially Magnetized ExB Plasmas in the Laboratory and Space

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Physics of Partially Magnetized ExB Plasmas in the Laboratory and Space

Low temperature, 10-50 eV partially magnetized plasmas

--naturally exist in ionosphere and solar plasma conditions

Created in laboratory and industry for material processing, film deposition (e.g. microelectronics), electric propulsion, ...

Partially magnetized: moderate magnetic field exist naturally (e.g. ionosphere) or created externally so that the electrons are magnetized, but ions are not

ExB - electric field exists (in space conditions), or is applied/created externally to control ions: confine/extract/accelerate ions (e.g. propulsion) for useful applications.

High temperature (>1 keV) plasmas: Tokamak, fusion, instabilities, turbulence and nonlinear waves, solitons, nonlinear physics, chaos, space physics, collisionless shock waves, ...



1980s:
Department of **Physics** and **Chemistry** of Plasmas
Moscow Institute of Physics and Technology
Kurchatov Institute, Moscow, Soviet Union



Low temperature (~ 10 eV) plasmas:
Physics of gas discharges... dominated by collisions,
Plasma chemistry — (too complex ...):
“ ..a wide but shallow sea” **L. Tsendin**
Море широкое, но мелкое ...
many applications, e.g. Plasma reactor for sulfur recovery from natural gas in Caspian sea deposits

In the meantime:

LTPSE- Low Temperature Plasma Science and Engineering –
Tremendous developments in scope and applications

LTPSE: ROBUST SCIENCE, SOCIETAL BENEFIT



01—Plasma TV

02—Plasma-coated jet turbine blades

03—Plasma-manufactured LEDs in panel

04—Diamondlike plasma CVD
eyeglass coating

05—Plasma ion-implanted artificial hip

06—Plasma laser-cut cloth

07—Plasma HID headlamps

08—Plasma-produced H₂ in fuel cell

09—Plasma-aided combustion

10—Plasma muffler

11—Plasma ozone water purification

12—Plasma-deposited LCD screen

13—Plasma-deposited silicon for
solar cells

14—Plasma-processed microelectronics

15—Plasma-sterilization in
pharmaceutical production

16—Plasma-treated polymers

17—Plasma-treated textiles

18—Plasma-treated heart stent

19—Plasma-deposited diffusion barriers
for containers

20—Plasma-sputtered window glazing

21—Compact fluorescent plasma lamp

- Operating premise:

LTPSE has a history and future of robust, interdisciplinary science challenges whose resolution provides immediate and long term societal benefit.

THE NATIONAL ACADEMIES

Advisers to the Nation on Science, Engineering, and Medicine

**Plasma 2010: Low Temperature Plasma
Science and Engineering**

M. Kushner, 2008, LTSP priorities and directions ...

Low temperature plasmas are becoming collisionless, magnetic field and nonlinear dominated!

V.A. Godyak, PoP 2005 Hot plasma effects in gas discharge plasma

M.A. Lieberman; V.A. Godyak, TPS IEEE 1998, From Fermi acceleration to collisionless discharge heating

A. Smolyakov, V. Godyak, PoP 2003 Nonlinear effects in inductively coupled plasmas

.....

V. Kolobov and V Godyak, PoP 2019, Electron kinetics in low-temperature plasmas

.. Experimental and theoretical advances reveal the importance of **nonlinear and kinetic phenomena in low-temperature plasmas (LTPs)**

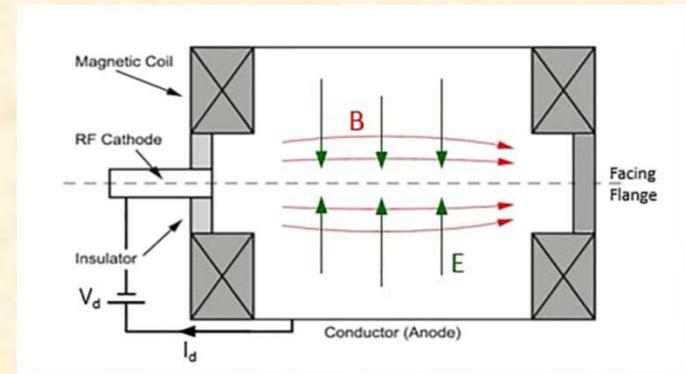
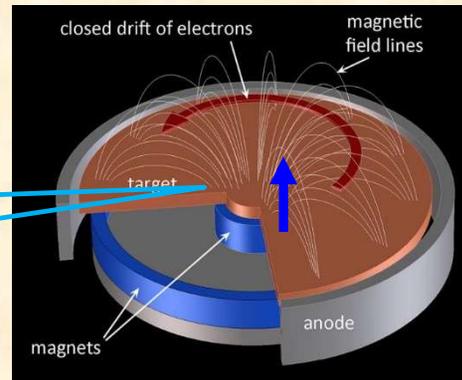
... Illustrate **common physics in space and laboratory plasma**, collisionless and collisional plasmas, and low-pressure and high-pressure discharges

... Nonlocal electron kinetics and nonlocal electrodynamics in low-pressure rf plasmas resembling **collisionless and nonlinear effects in space plasma and hot plasma effects in fusion science**, terahertz technology, and plasmonics.

Common physics in laboratory, industrial material processing, electric propulsion and space plasmas.

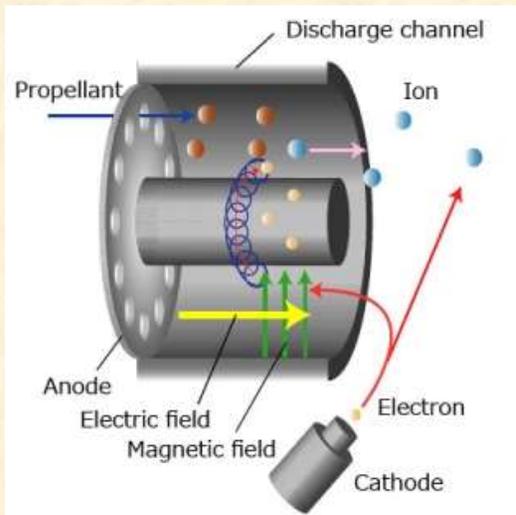
Devices: magnetrons, Penning discharge, magnetic filters, Hall thrusters ,

E electric field



Planar magnetron, A. Anders, J App Phys 2017

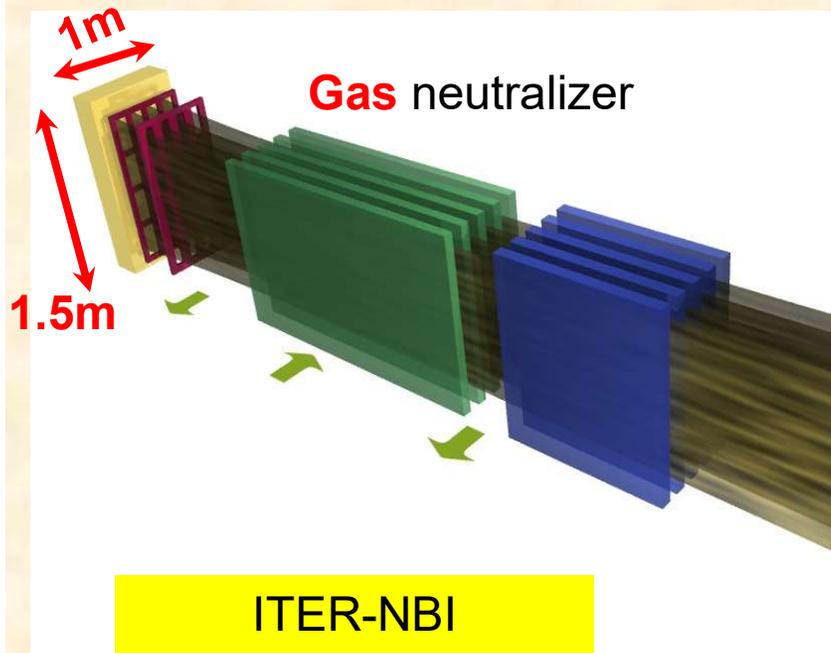
Hall thruster



Cylindrical Penning discharge,
Y. Raitses PPPL,
From Rodrigues et al, PoP 2019

Magnetic filter for negative ion beam source

Objectives: increase the injector efficiency



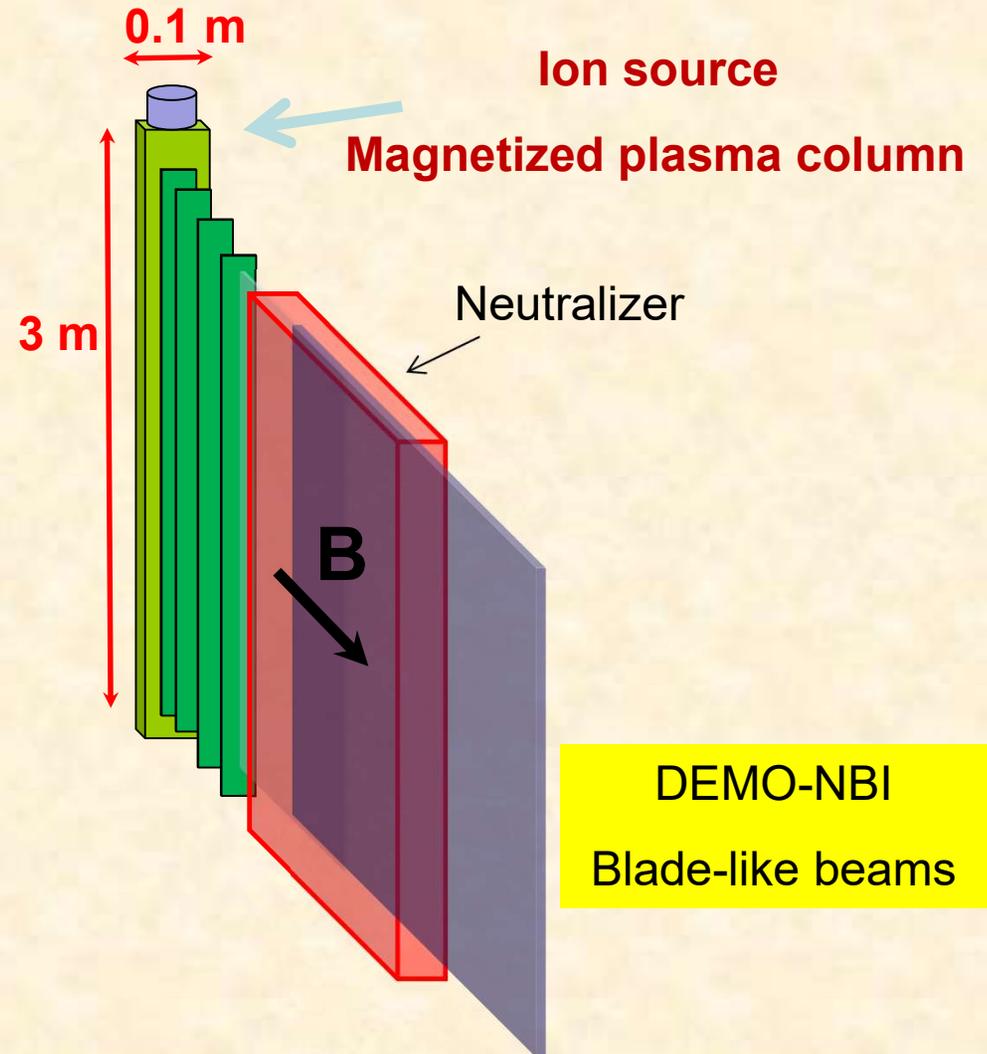
ITER-NBI

Square aspect ratio

Significant beam losses

Poor injector efficiency (< 25 %)

G Fubiani



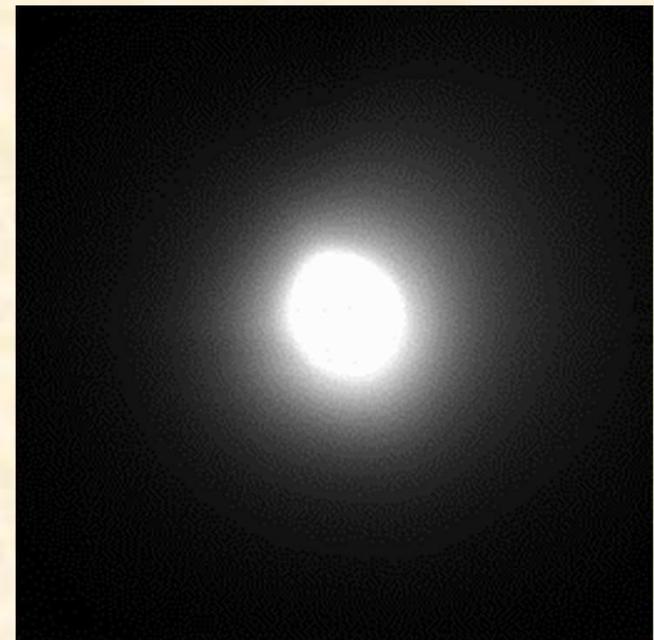
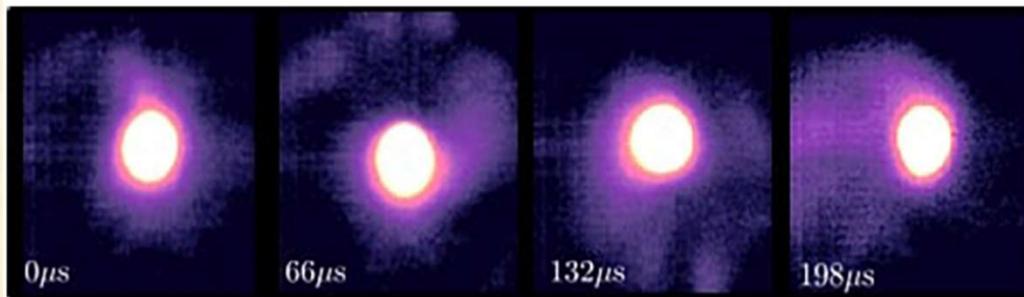
DEMO-NBI

Blade-like beams

Physics of ExB plasmas addresses (among other problems):

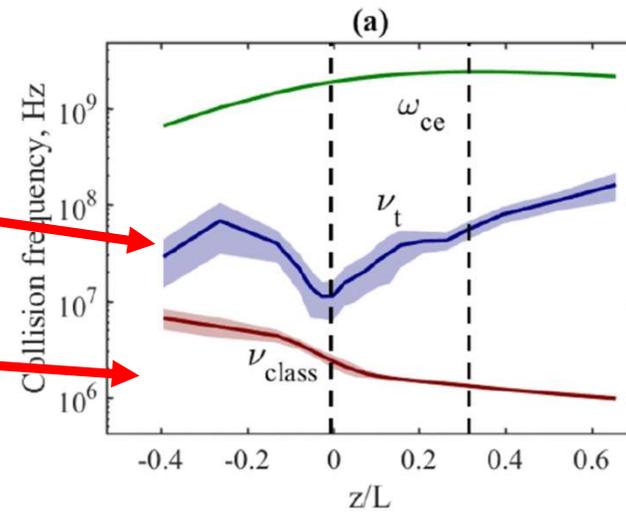
- **Range of unstable fluctuations** of different frequencies and scale ubiquitously observed in Hall thrusters, magnetrons, and similar devices
- **Electron transport** across the magnetic field is anomalous.
- **Large scale coherent structures** (spoke)
- Fluctuations across different time and length scales, have **dramatic effects** on **underlying regimes and performance** of various devices (10 kHz-1 MHz and higher)
- Nature of fluctuations and transport is **poorly understood**, precludes first principle predictive modeling

Rotating spoke in Penning discharge, Rodrigues et al, PoP 2019



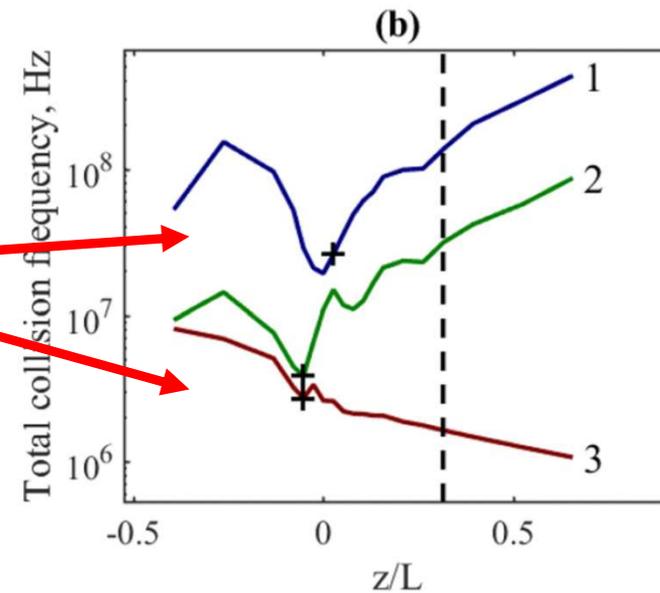
Experiments on mobility

Electron current is **anomalous**,
orders of magnitude above the
classical



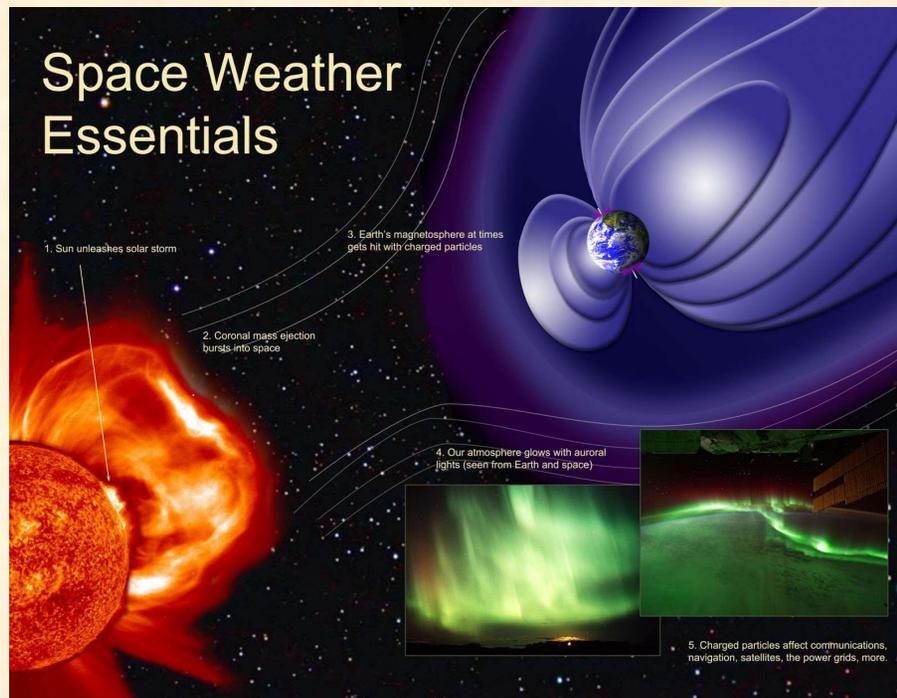
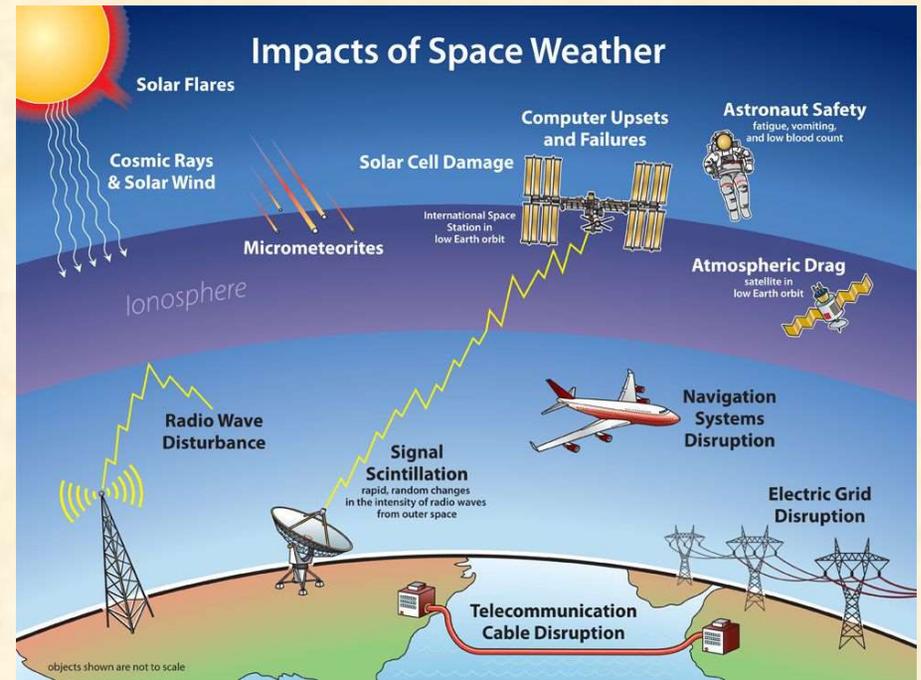
Effective (total) collision frequency in Hall thruster,
E. Dale, B Jorns, PoP 2019

Anomalous electron current is
modulated by the lower frequency
(~ 10 kHz) breathing mode cycle



E. Dale, B Jorns, PoP 2019

Plasma fluctuations and structures (**irregularities**) in space weather



Space weather is a branch of [space physics](#) and [aeronomy](#), or [heliophysics](#), concerned with the time varying conditions within the Solar System, including the [solar wind](#), emphasizing the space surrounding the Earth, including conditions in the [magnetosphere](#), [ionosphere](#), [thermosphere](#), and [exosphere](#). ...

https://en.wikipedia.org/wiki/Space_weather

Ionosphere irregularities



Super Dual Auroral Radar Network (SuperDARN) Facility for studies of ionosphere irregularities (Coherent Radar Scattering), near Saskatoon SK

Photo credit: A Reimer, Ph D student, Department of Physics and Engineering Physics , University of Saskatchewan

Partially magnetized $\mathbf{E} \times \mathbf{B}$ plasmas (Hall plasmas)

- Configuration with perpendicular electric and magnetic fields, $\mathbf{E}_0 \perp \mathbf{B}_0$
- Magnetized electrons $\omega < \omega_{ce}$ $\rho_e < L$
- Un-magnetized ions $\rho_i > L$
- Magnetic filter: electrons are trapped; motion across the magnetic field is constrained, drifting $\mathbf{V}_E = \mathbf{E} \times \mathbf{B} / B^2$
- **Ions are weakly affected by the magnetic field; controlled by the electric field; can be accelerated/extracted, etc,...**

Problem

Fluctuations, structures and anomalous transport in ExB plasmas:

- Ubiquitously observed in many devices
- Multi-scale nonlinear problem: small scales are typically most unstable, can feed large scale structures; large scale structures modify the equilibrium and affect stability conditions for small scales: self-organization

Long wavelength modes dominantly contribute to the anomalous transport/current (e.g. large fraction of the current may go via spoke structure)

$$D \approx \frac{(\Delta x)^2}{\tau} \sim \frac{\lambda^2}{\lambda} \sim \lambda$$
$$\tau \sim \gamma^{-1}$$
$$\gamma \sim kc_s \sim 1/\lambda$$

Approach, methods and tools

First principle physics (analytical) models

Analysis of linear eigen-modes and instabilities

Reduced analytical and nonlinear simulations models

Fluid and kinetic numerical simulations

Verification, e.g. codes bechmarking and validation with experiments

2D reduced (azimuthal-axial) fluid turbulence code

2D kinetic (particle-in-cell) codes (azimuthal-axial, azimuthal-radial)

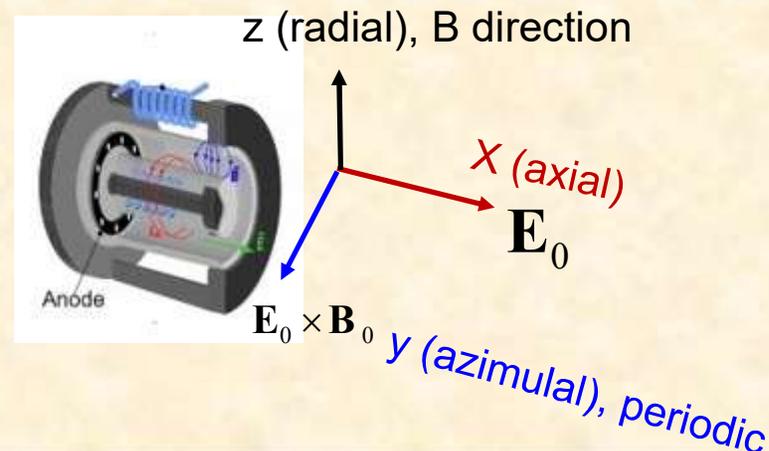
1D fluid and 1D hybrid (kinetic ions and neutrals) codes for ionization/breathing modes

1D Vlasov (direct-kinetic) turbulence code

Next:

- Eigen-modes and instabilities
 - Gradient-drift (Simon-Hoh) modes
 - Lower hybrid modes
 - Resistive, axial (along the applied \mathbf{E}_0) modes
- Advanced fluid model and simulations
 - Inverse cascade, self-organization and coherent structures: zonal flows, vortices and streamers
 - Anomalous current
- Kinetic effects and simulations

} Azimuthal modes
along $\mathbf{E}_0 \times \mathbf{B}_0$



Confined plasmas has gradients

→ Density, temperature, magnetic field are inhomogeneous
also electric field is a part of the equilibrium

→ Gradients induce waves -- drift waves
and instabilities

→ Drift waves in partially magnetized plasma are
different from e.g. tokamak (fully magnetized)

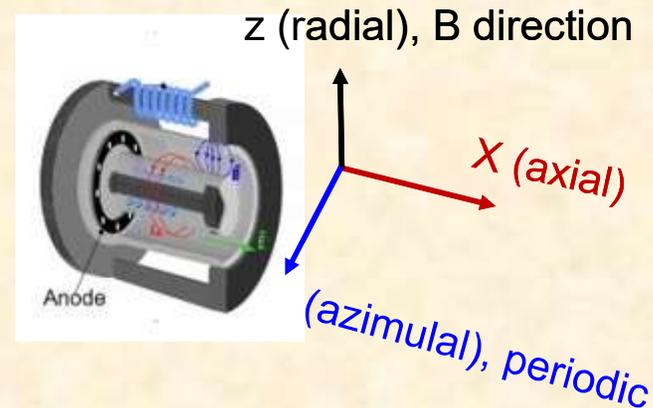
Drift mode in partially magnetized plasma

- Gradient effects in electron dynamics

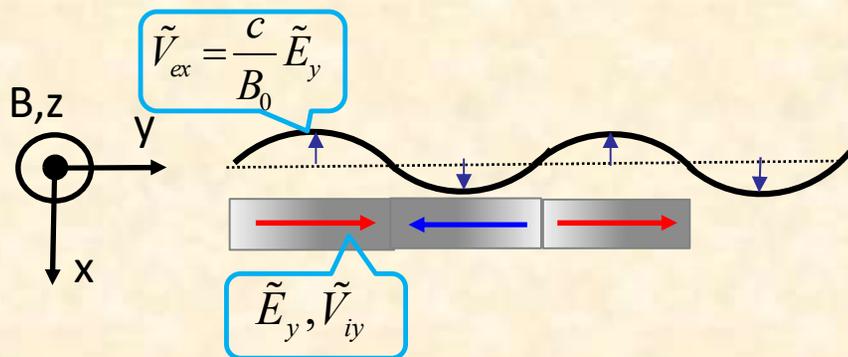
$$\frac{\partial}{\partial t} \tilde{n} + \tilde{V}_E \cdot \nabla n_0 = \frac{\partial}{\partial t} \tilde{n} + \frac{c}{B_0} \tilde{E}_y \frac{\partial n_0}{\partial x} = 0$$

- Unmagnetized ions

$$\frac{\partial \tilde{V}_y}{\partial t} = \frac{e}{m_i} \tilde{E}_y$$



- “Anti-drift mode” (Fridman, 1964)



$$\omega = -k_y \omega_{ci} L_n = \frac{k_y^2 c_s^2}{\omega_*}$$

$$\omega_* = -\frac{k_y c T_e n_0'}{e B n_0}$$

Gradient-drift/Simon-Hoh instability in ExB plasma

- Electron dynamics with $\mathbf{V} = c\mathbf{E} \times \mathbf{B} / B^2 = -cE_{0x} / B_0 \hat{y}$ electron flow
Simon-Hoh instability: Negative compressibility/negative energy

$$\omega^2 = k_y^2 \omega_{ci} V_{0y} L_n < 0$$

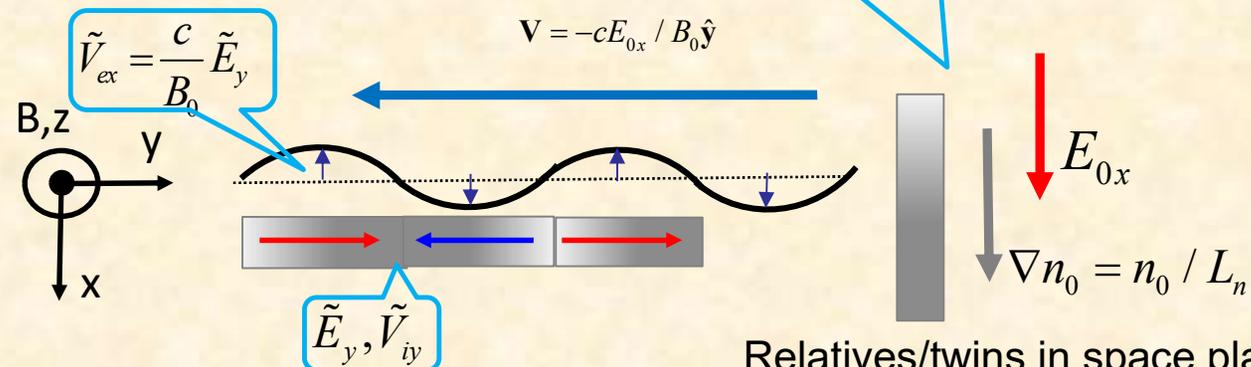
$$\gamma = k_y \sqrt{\frac{eE_{0x} L_n}{m}}$$

$$\frac{\partial p}{\partial n} = -eE_{0x} \left(\frac{1}{n_0} \frac{\partial n_0}{\partial x} \right)^{-1} = -eE_{0x} L_n < 0$$

Modified by magnetic field gradients

$$\nabla n \rightarrow \nabla(n / B^2)$$

aka Rayleigh-Taylor instability of the stratified density in the gravity field (heavy fluid on top)

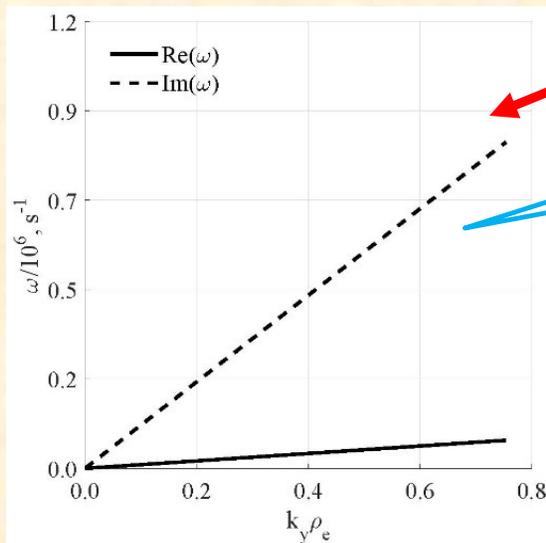


Relatives/twins in space plasma:
gradient-drift and Farley-Buneman instabilities

Simon, Hoh, ..., 60s, Huba, .. Sakawa, 1992,
Morozov, Esipchuk, Tilinin, 60s, Cappelli, Ahedo, Kapulkin Raitses,...

Inertia modification of the Simon-Hoh instability?

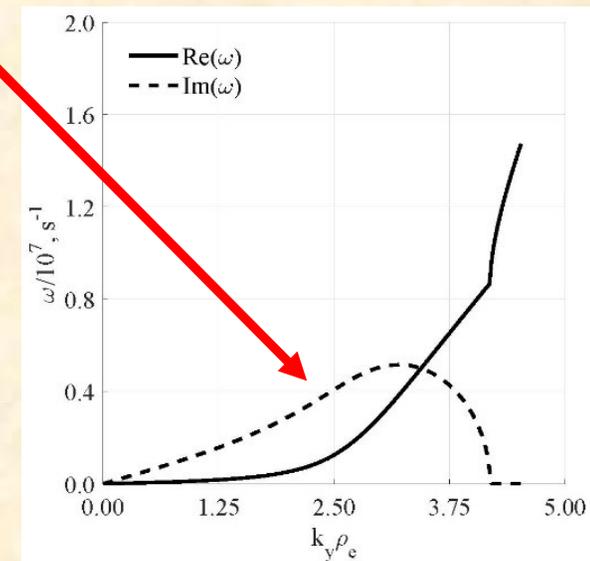
Electron inertia brings new mode (lower-hybrid) and provides the physics based cut-off at high wavelengths –lower-hybrid instability



Growth rates

Without inertia

With inertia



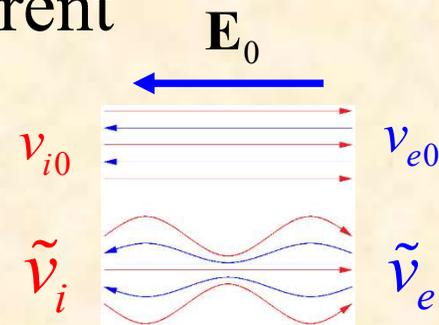
“High frequency” ion sound: short wavelength extension of the lower-hybrid mode

$$\omega^2 = \omega_{LH}^2 \left(1 + k_{\perp}^2 \rho_e^2 \right) \approx \omega_{LH}^2 k_{\perp}^2 \rho_e^2 = k_{\perp}^2 c_s^2$$

Resistive current flow (axial) instability

Driven by the axial ion/electron current. Phase shift between the ion inertial (ballistic) and electron dissipative response. Electron anomalous current can serve the role of the dissipative current

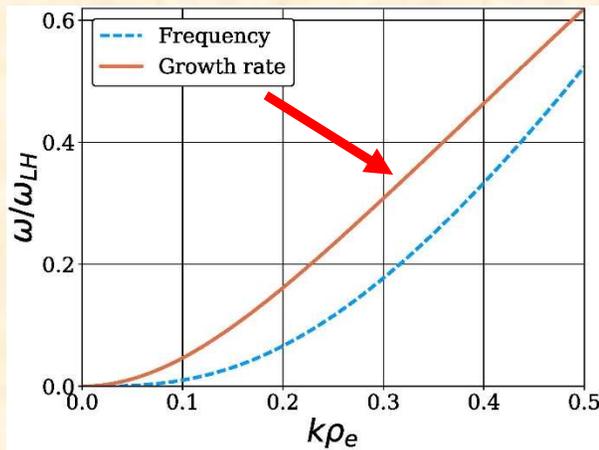
Inherent instability of the current flow due to the phase shift between the dissipative response of the electron flow and ballistic (inertial) response of ions



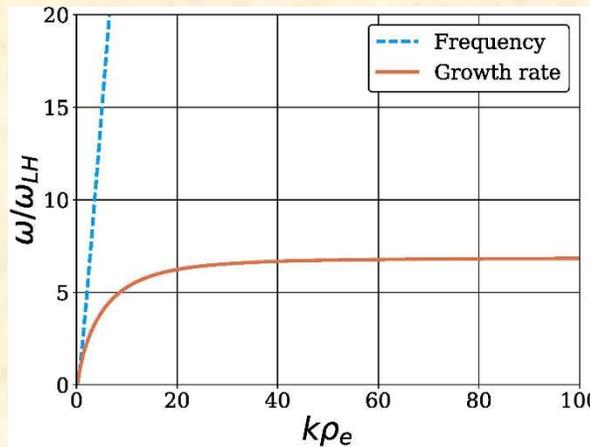
Chable, Rogier, 2005
Fernandez et al 2008
Koshkarov et al, 2017, 2018

Electron current: $\mathbf{J}_e = \sigma_{\perp} \mathbf{E}_0$
collisional and/or anomalous

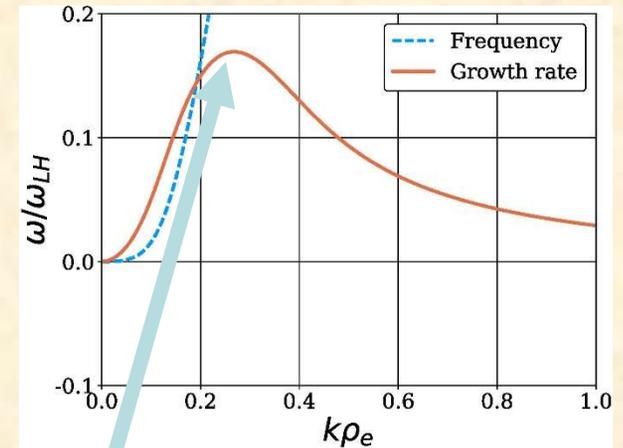
Electron inertia selects the most unstable mode



Growth rates: without inertia



with diffusion but without inertia



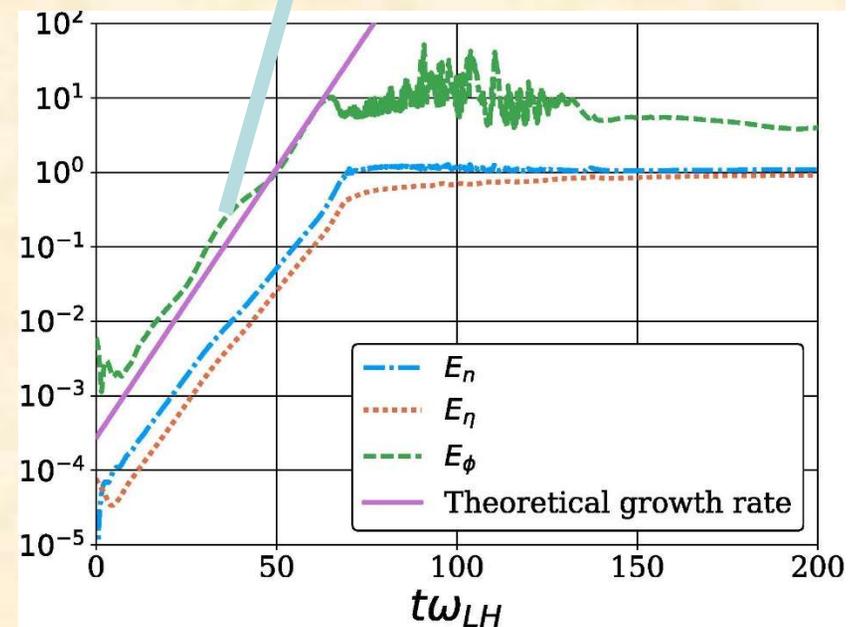
with inertia

The mode is long-wavelength!

$$\gamma \approx \nu \frac{k_x^2 v_{0i}^2}{\omega_{LH}^2}$$

Linear growth and nonlinear saturation of axial resistive modes.

Koshkarov et al, Physics of Plasma 2017, 2018



Advanced fluid model for nonlinear simulations

- **Unmagnetized ions**
- **Reduced model for magnetized electrons, expansion in small**
 - **parameters** $\omega_{ce} > (\omega, v_e, k_{\perp} V_{\perp})$
 - **Finite electron radius effects are included, good agreement with kinetic theory, Pade approximants for large $k_{\perp} \rho_e \gg 1$**
 - **Density gradient mode** $\omega = -\omega_{ci} k_y L_n$, **destabilized by $\mathbf{E} \times \mathbf{B}$ flow (Simon-Hoh**
 - **Electron inertia and lower-hybrid modes**
 - **Resistive instabilities and ion flow destabilization**

Reduced nonlinear equations:

$$\omega_{ce}^{-1} \partial / \partial t \ll 1$$

Electrons

Density gradient,
Simon-Hoh

Magnetic field
gradient

Collisions

$$\frac{\partial n}{\partial t} + \frac{c}{B} \{\phi, n\} + \mathbf{v}_E \cdot \nabla n_0 - 2n \mathbf{v}_E \cdot \nabla \ln B - 2n \mathbf{v}_{pe} \cdot \nabla \ln B + \frac{\nu c n_0}{B_0 \omega_{ce}} \nabla_{\perp}^2 \left(\phi - \frac{T_e}{e n_0} n \right) + \frac{n_0 c}{\omega_c B_0} \left(\frac{\partial}{\partial t} + \mathbf{v}_E \cdot \nabla \right) \nabla_{\perp}^2 \phi + \frac{c^2 T_e}{e B^2 \omega_{ce}} \nabla \cdot \{ \nabla \phi, p \} = 0$$

inertia

Ion flow

Ions

$$\tilde{\mathbf{v}} = -\nabla \tilde{\chi}$$

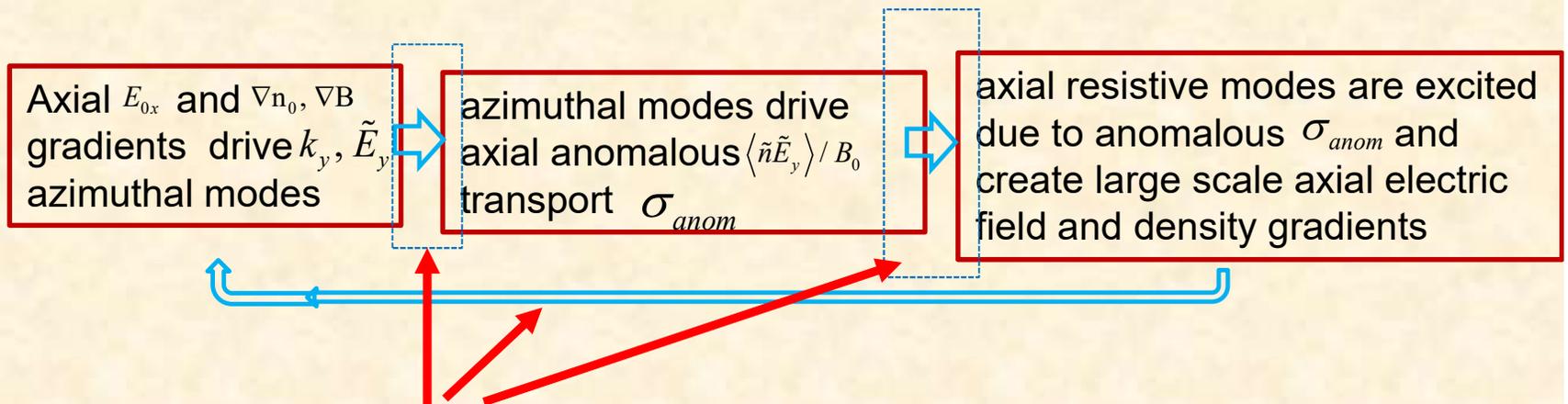
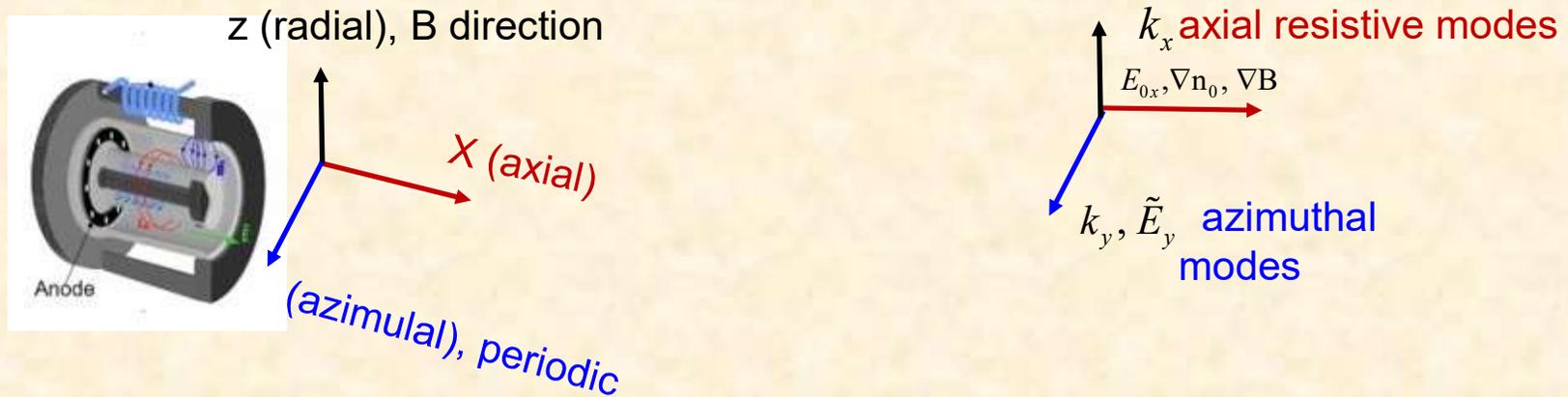
$$\frac{\partial}{\partial t} \nabla^2 \tilde{\chi} = \nabla^2 \left(\frac{e}{m_i} \phi + \frac{(\nabla \tilde{\chi})^2}{2} \right) - v_0 \frac{\partial}{\partial z} \nabla^2 \tilde{\chi} - 2 \frac{\partial v_0}{\partial z} \frac{\partial^2 \tilde{\chi}}{\partial z^2} - \frac{\partial \tilde{\chi}}{\partial z} \frac{\partial^2 v_0}{\partial z^2}$$

$$\left(\frac{\partial}{\partial t} + \mathbf{v}_0 \cdot \nabla \right) \tilde{n} - \nabla \tilde{\chi} \cdot \nabla n_0 + \tilde{n} \nabla \cdot \mathbf{v}_0 - n_0 \nabla^2 \tilde{\chi} - \nabla \cdot (\tilde{n} \nabla \tilde{\chi}) = 0.$$

2D: azimuthal-axial, includes ion flow

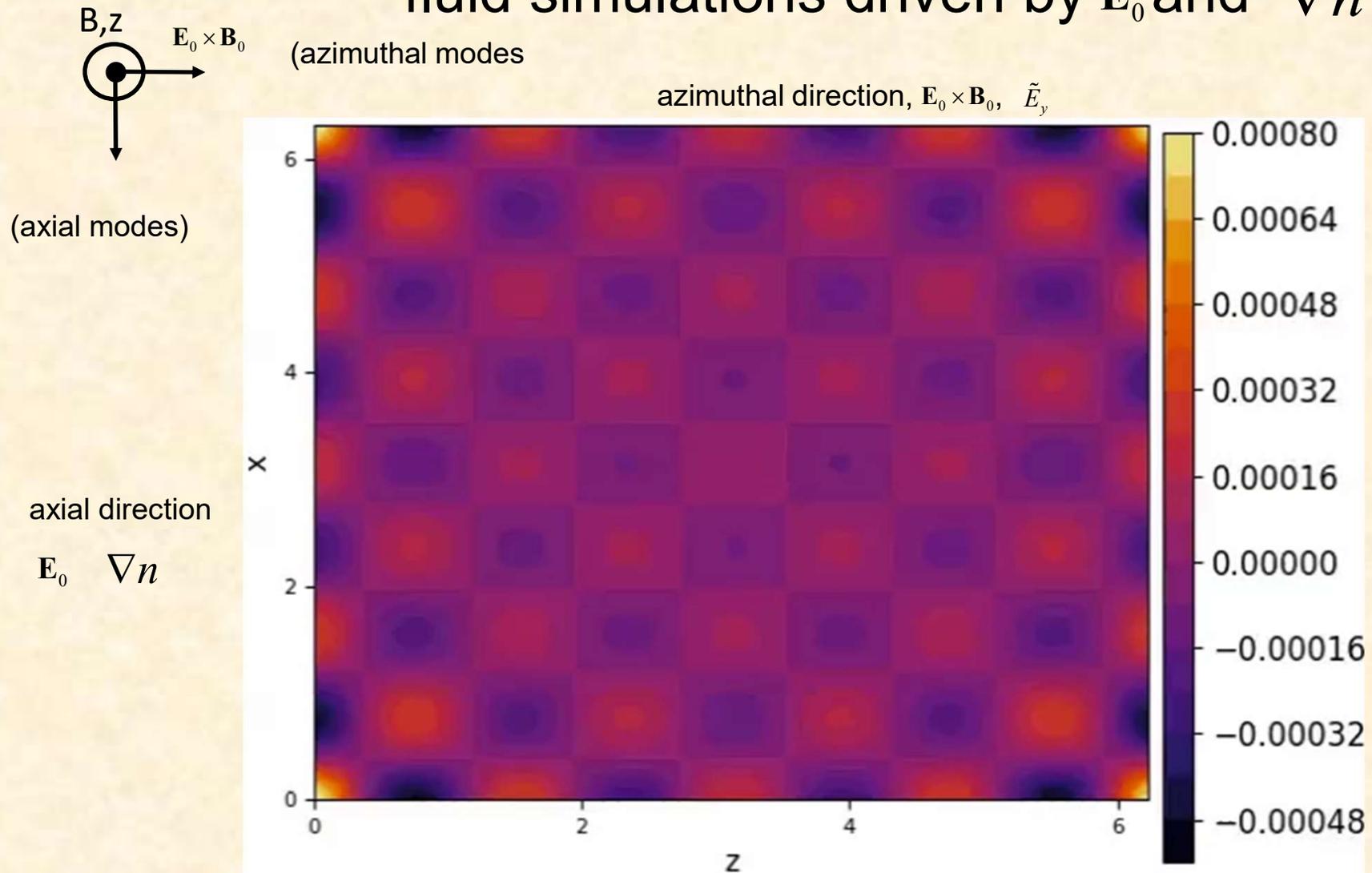
Smolyakov et al.,
Plasma Physics and Controlled Fusion, 2016

Self-organization in partially magnetized ExB plasma

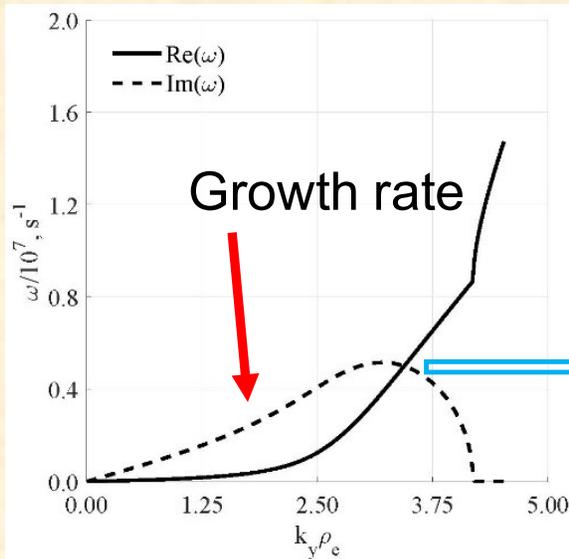


This coupling has been demonstrated in reduced simulations

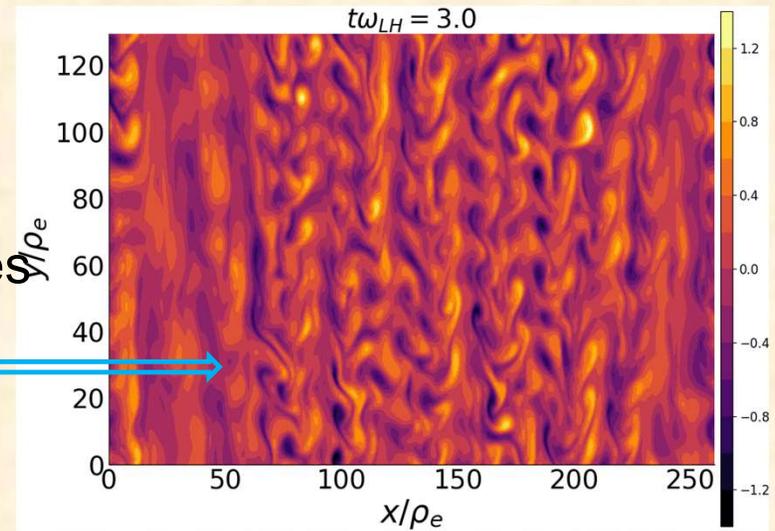
Turbulence, transport and structures in nonlinear fluid simulations driven by \mathbf{E}_0 and ∇n



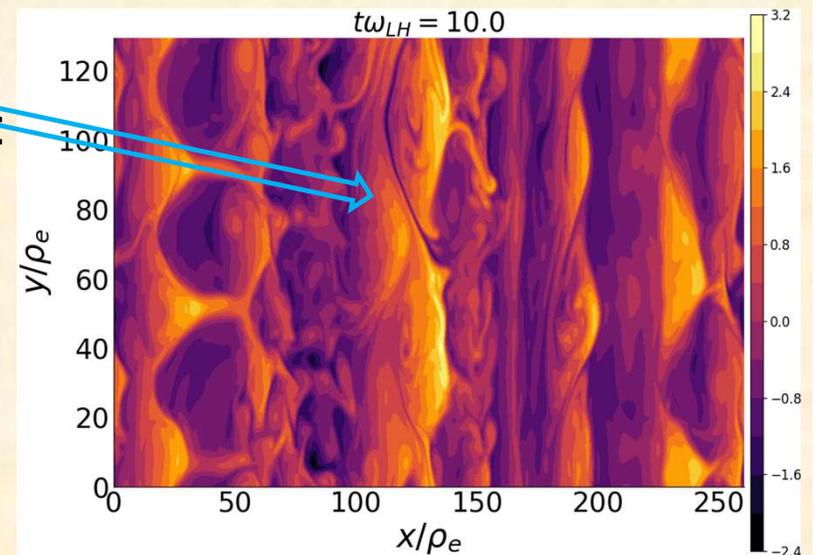
Energy cascades from high k (most unstable) to low k (box size) modes: inverse cascade



Most unstable small scale modes



Large scale structures in saturated state

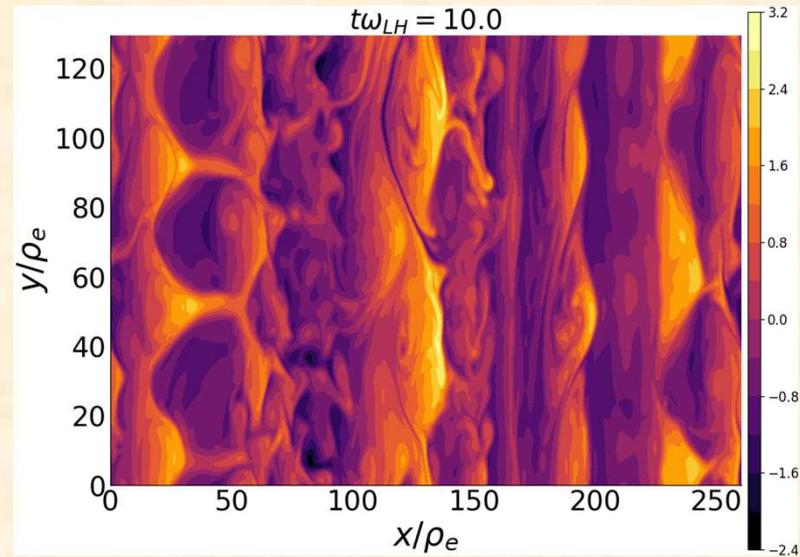
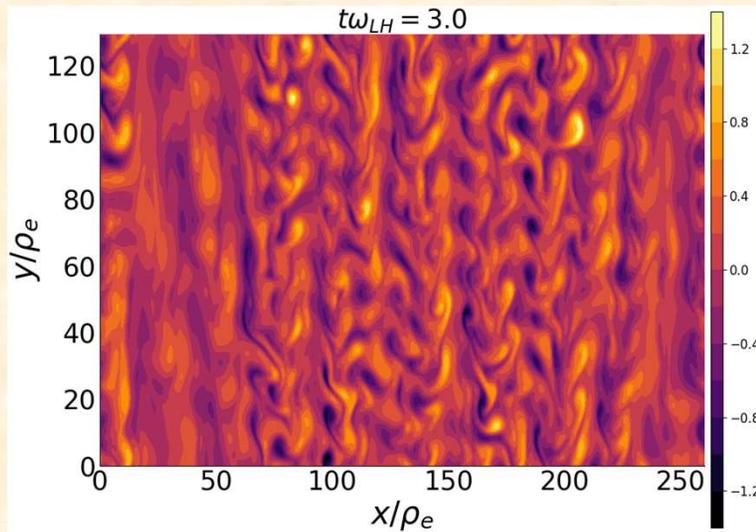


Inverse cascade is a signature of 2D systems:
Nonlinear terms from electron inertia

$$\mathbf{V}_e = \dots + \frac{\mathbf{B}}{\omega_{ce} B} \times \left(\frac{\partial}{\partial t} + \mathbf{V}_E \cdot \nabla + \mathbf{V}_{pe} \cdot \nabla \right) \mathbf{V}$$

Nonlinear excitation of long-wavelength modes in Hall plasma, Lakhin, Ilgisonis, Smolyakov PoP 2016

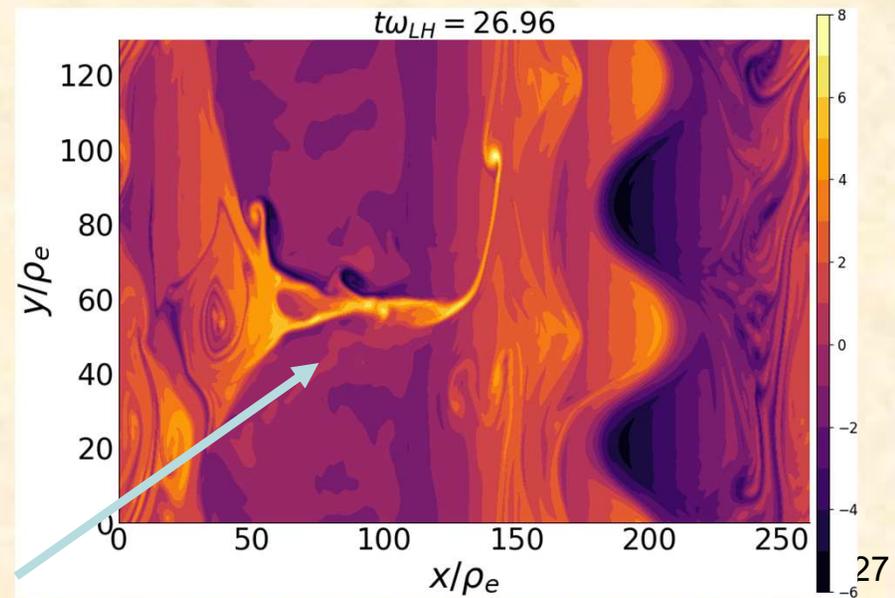
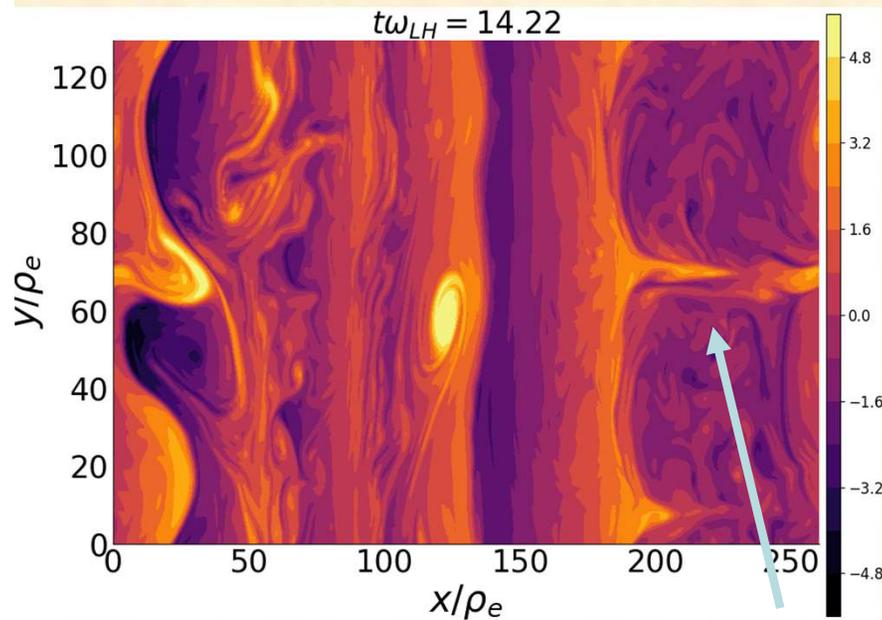
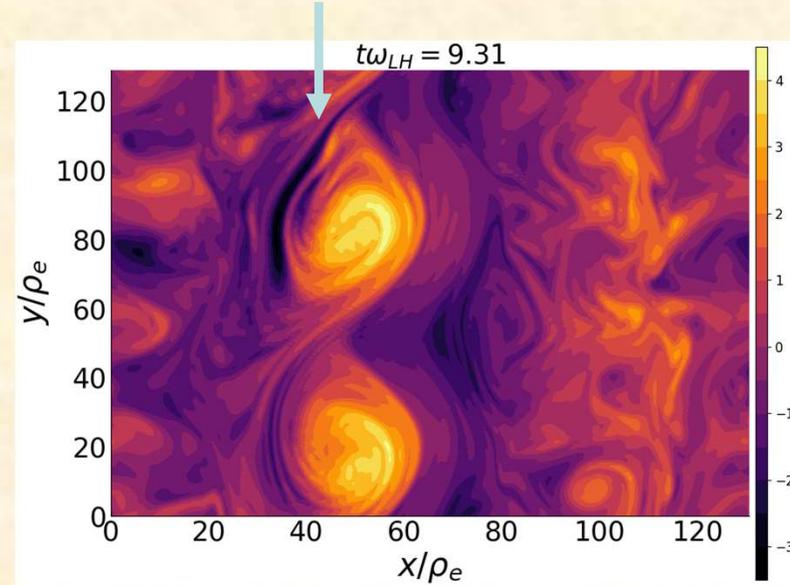
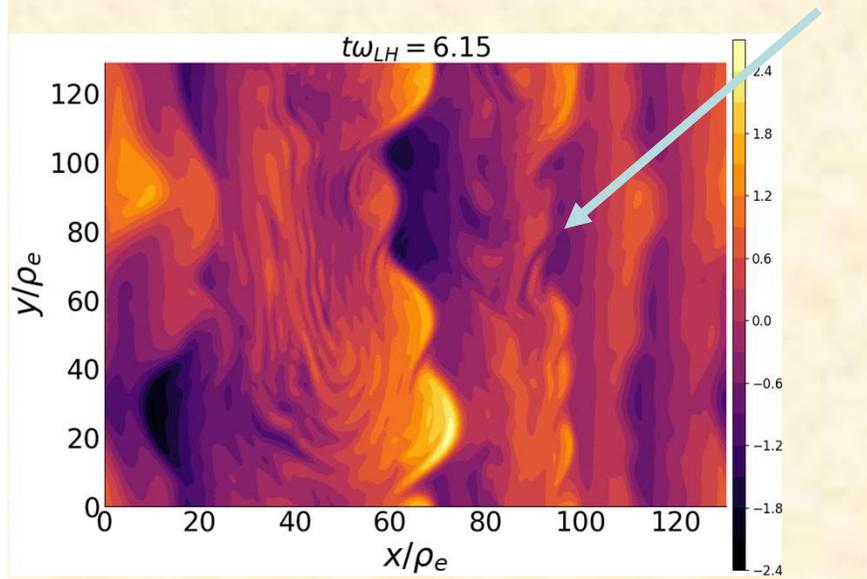
Inverse cascade -> zonal flows and vortex structures



Zonal flows and
Great Red Spot
on Jupiter

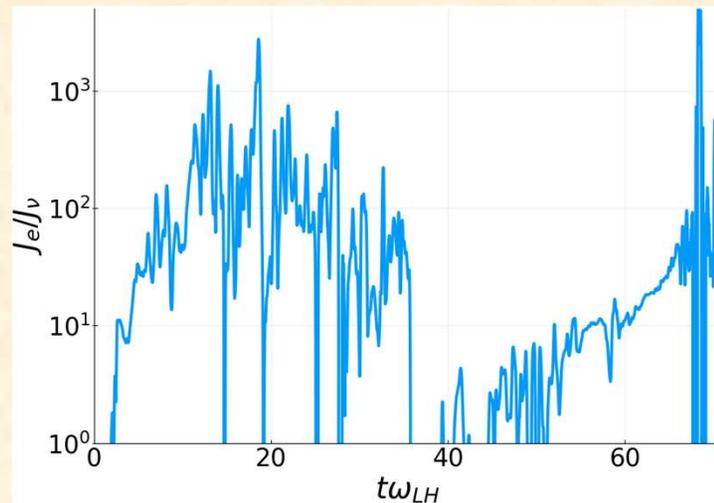


Self-organization: zonal flows, vortices and streamers



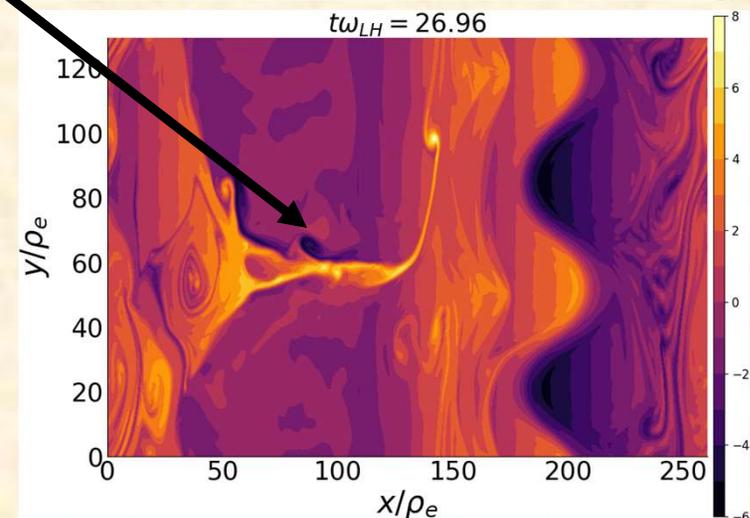
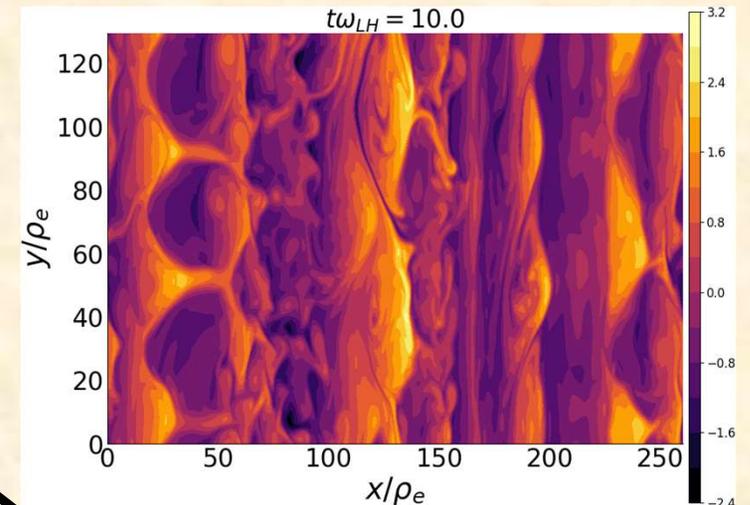
streamers

- First principle self-consistent demonstration of the anomalous conductivity in fluid simulations
- Inverse cascade, self-organization and formation of large scale structures from small scale turbulence



Zonal flow
and vortices

Streamer



- Large anomalous current: effective Hall parameter $\sim 27-50$;
- Highly intermittent: not diffusive process (of many small events); rather like sequence of relatively rare but large transport events)
- Self-organized criticality (avalanche occurs near the critical state)
- Does parameterization of anomalous current by mobility apply here?

Kinetic effects and Instabilities in $E \times B$ discharges

- **Electron Cyclotron Drift Instability (ECDI):**

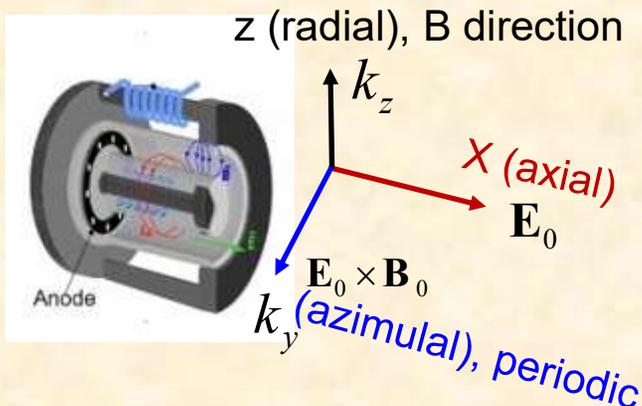
⇒ Strong electric field. **Cyclotron resonance driven (collisionless). No density, magnetic field and other gradients are required,** k_y along $\mathbf{E}_0 \times \mathbf{B}_0$

- **Electron Drift Instability (EDI)**

⇒ Strong electric field. ECDI modified by **nonlinear and other effects**, e.g. turbulence broadening, ion sound, etc
 k_y along $\mathbf{E}_0 \times \mathbf{B}_0$

- **Modified Two Stream Instability (MTSI)**

⇒ Strong electric field. Electron motion along the magnetic field is included + Doppler shift along $\mathbf{E}_0 \times \mathbf{B}_0$, k_y and k_z



Magnetized electrons $\mathbf{E}_0 \times \mathbf{B}_0$ beam streaming with respect to unmagnetized (stationary) ion – aka two-stream instability

Electron Cyclotron Drift, Modified

Two-Stream Instabilities and Buneman (magnetized plasma) instabilities

In cold plasmas

Buneman, 1962

$$1 - \frac{\omega_{pi}^2}{\omega^2} - \frac{\omega_{pe}^2}{(\omega - k_y V_E)^2 - \omega_{ce}^2} - \frac{k_z^2}{k^2} \frac{\omega_{pe}^2}{(\omega - k_y V_E)^2} = 0$$

Buneman

Modified two-stream

With warm electrons, sequence of resonances, $m=1,2,3..$

$$\omega - k_y v_0 - m\omega_{ce} \approx 0$$

$$1 + K_i + K_e = 0 \quad K_i = -\frac{\omega_{pi}^2}{\omega^2}$$

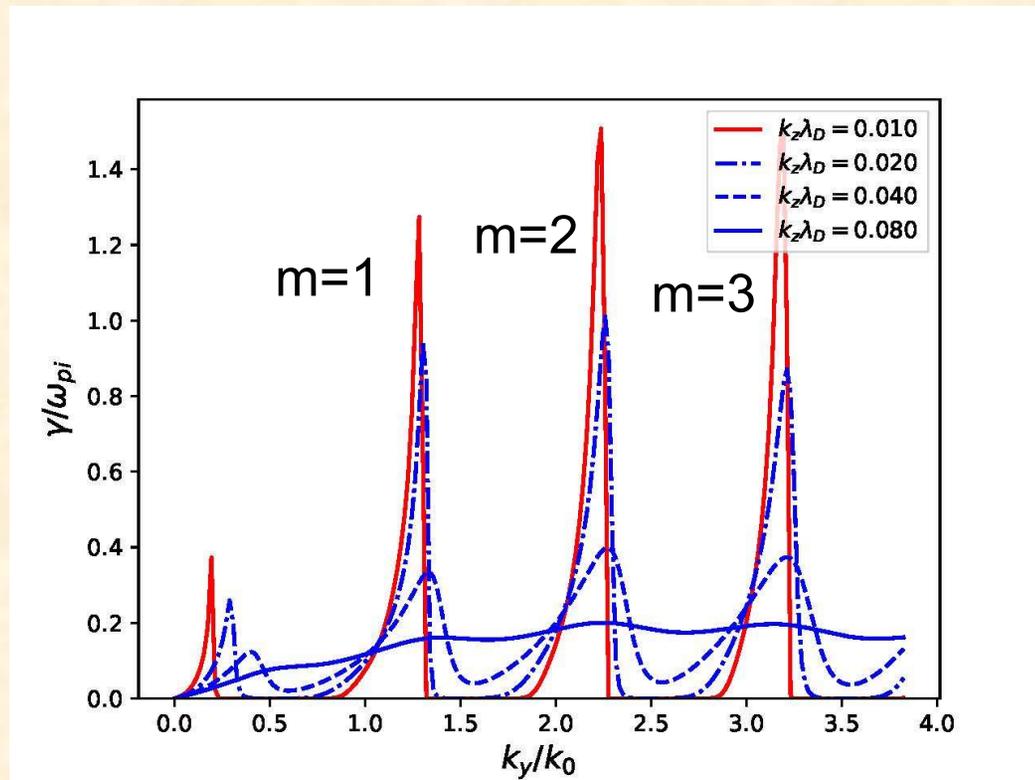
$$K_e = \frac{1}{k^2 \lambda_D^2} \left[1 + \frac{\omega - k_y v_0}{\sqrt{2} k_z v_{Te}} \sum_{m=-\infty}^{\infty} I_m(k_{\perp}^2 \rho_e^2) \exp(k_{\perp}^2 \rho_e^2) Z\left(\frac{\omega - k_y v_0 - m\omega_{ce}}{\sqrt{2} k_z v_{Te}}\right) \right]$$

Electron cyclotron drift instability

$$\omega - k_y v_{ExB} = m\omega_{ce}$$

$m=1, 2, 3..$ resonances

$$\omega \ll k_y v_{ExB} \sim m\omega_{ce}$$



Recent history

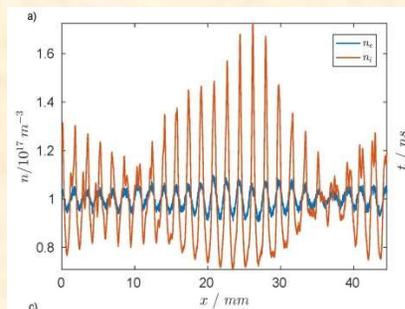
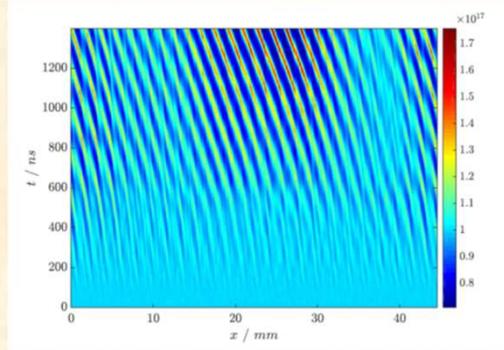
ECDI in ExB discharges, Hall thrusters and magnetron applications

- PIC simulations: Adam, Heron 2004, 2006, ..., 2013; Ducroq 2006
- Tsikata- 2009, 2011, 2015... Collective light scattering measurements, Magnetron -2015
- Lafleur, Baalrud... 2016, 2017; quasilinear estimates
- Katz, Mikellides 2015 – applied to HT
- Lafleur 2017, Croes 2017 – R- θ PIC simulations
- Boeuf 2013, 2015, 2017 –review in J Appl Phys
- Charoy et al 2019
-

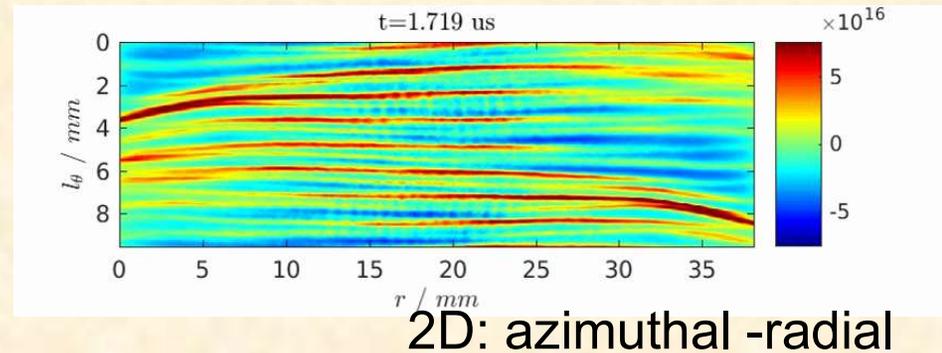
Coherent modes in 1D and 2D simulations

Lafleur et al. 2016, Boeuf .. 2017, Janhunen et al, Phys Plasmas 2018a,b;
Zintel... 2019, Charoy et 2019, Taccogna 2019

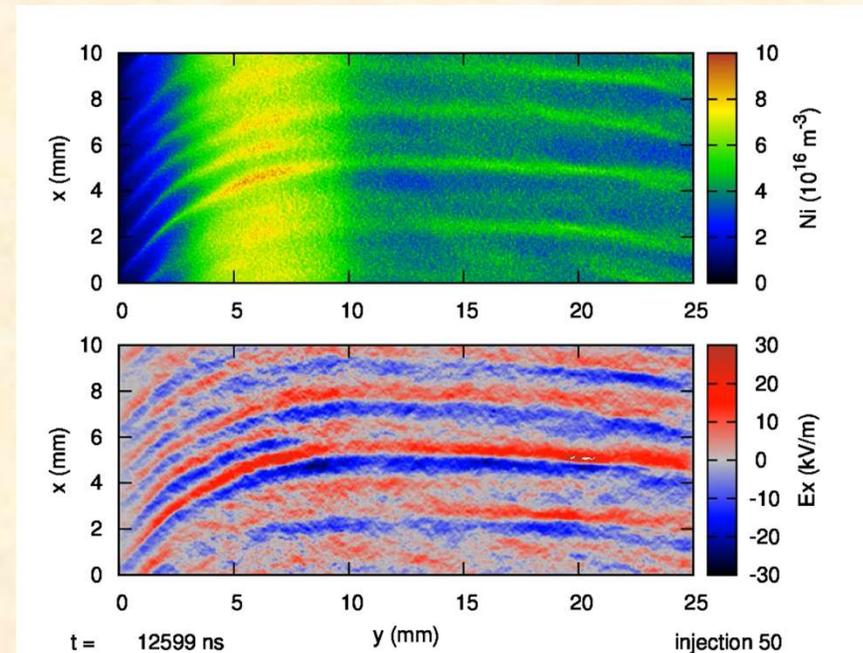
Long wavelength condensation



1D azimuthal



2D: azimuthal -radial

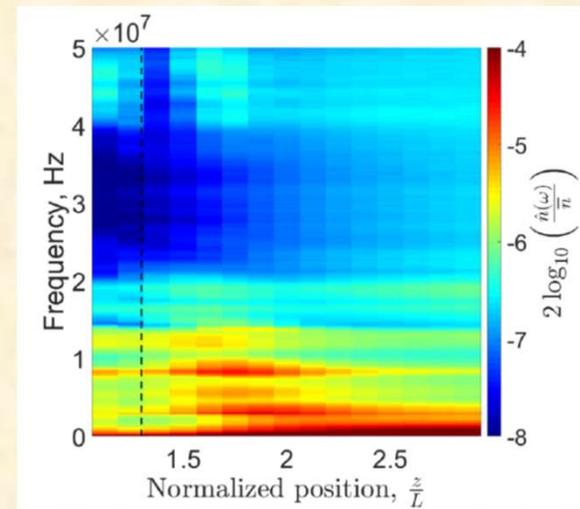
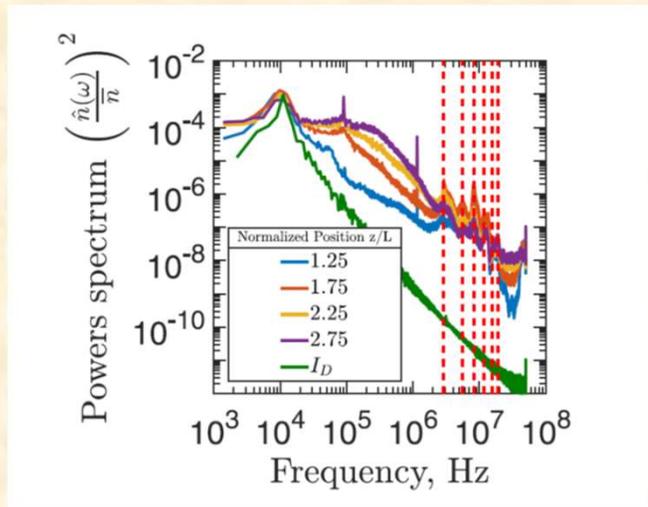
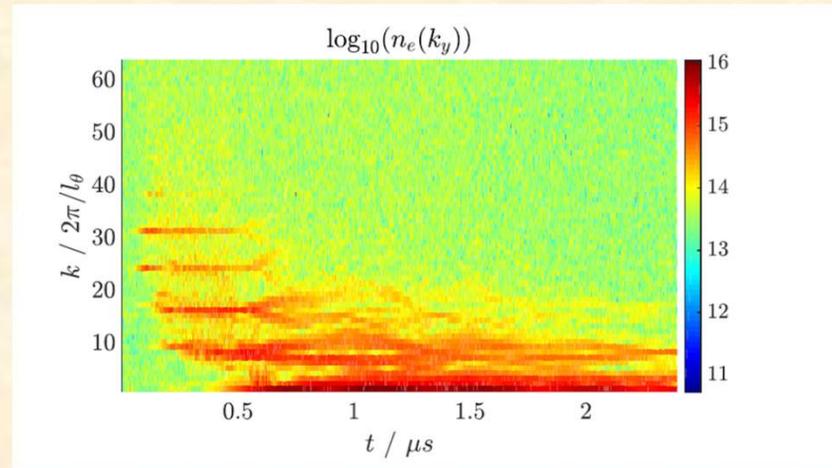


2D: azimuthal -axial

Cyclotron resonances and inverse cascade to longer wavelengths

Resonances and condensation toward the long wavelength

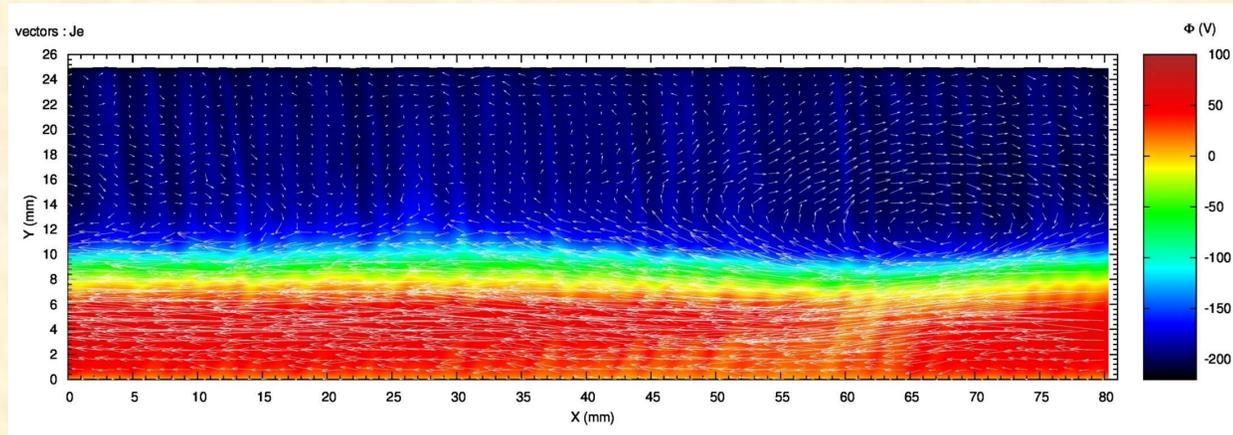
S Janhunen, Smolyakov et al. 2018



Resonances and long wavelength condensation in experiment

Z Brown, B Jorns, PoP 2019

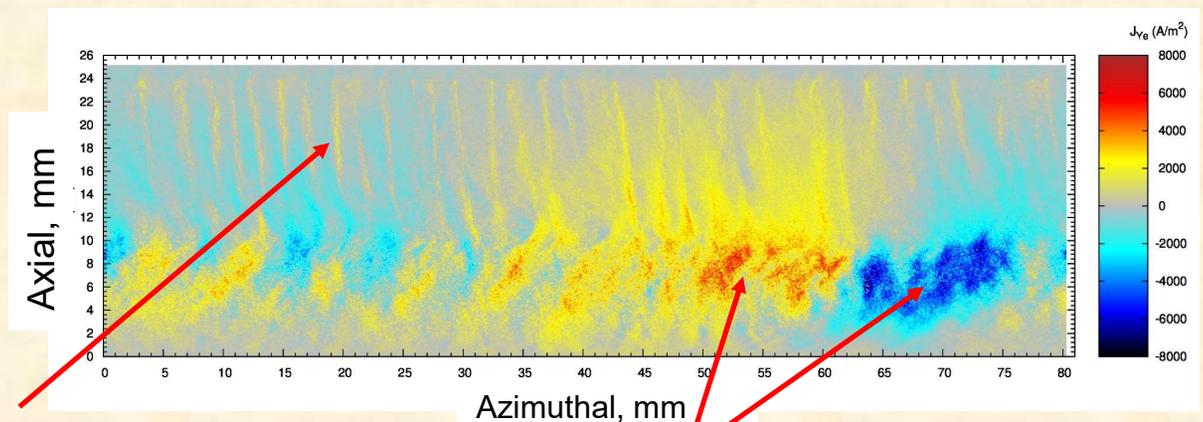
Inverse cascade: Current streamers and current vortices in large box simulations



Electron current forms a vortex (or two) in the transport region (almost zero electric field)

Sydorenko, Smolyakov, Tavasoli 2021

Coherent structures
in current!

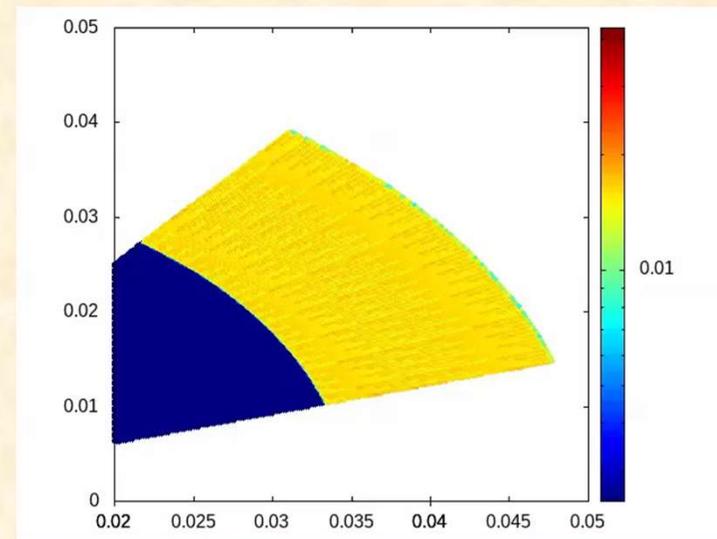
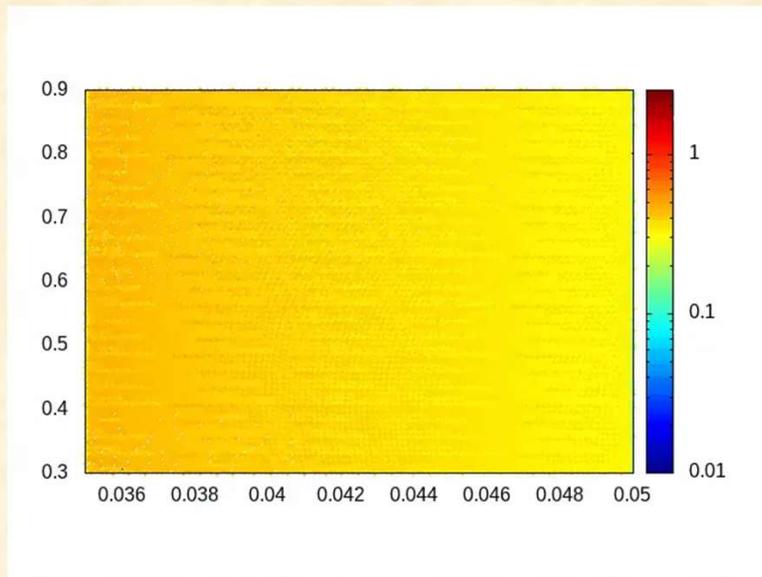
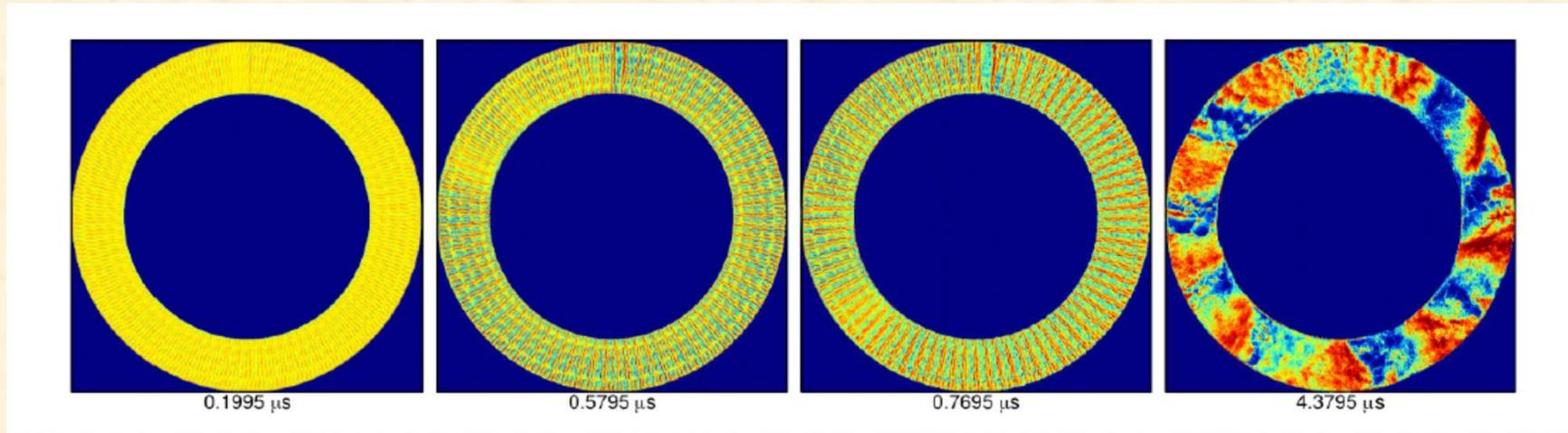


Current streamers

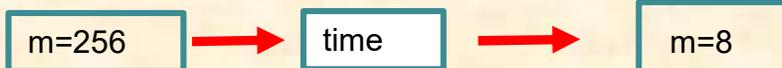
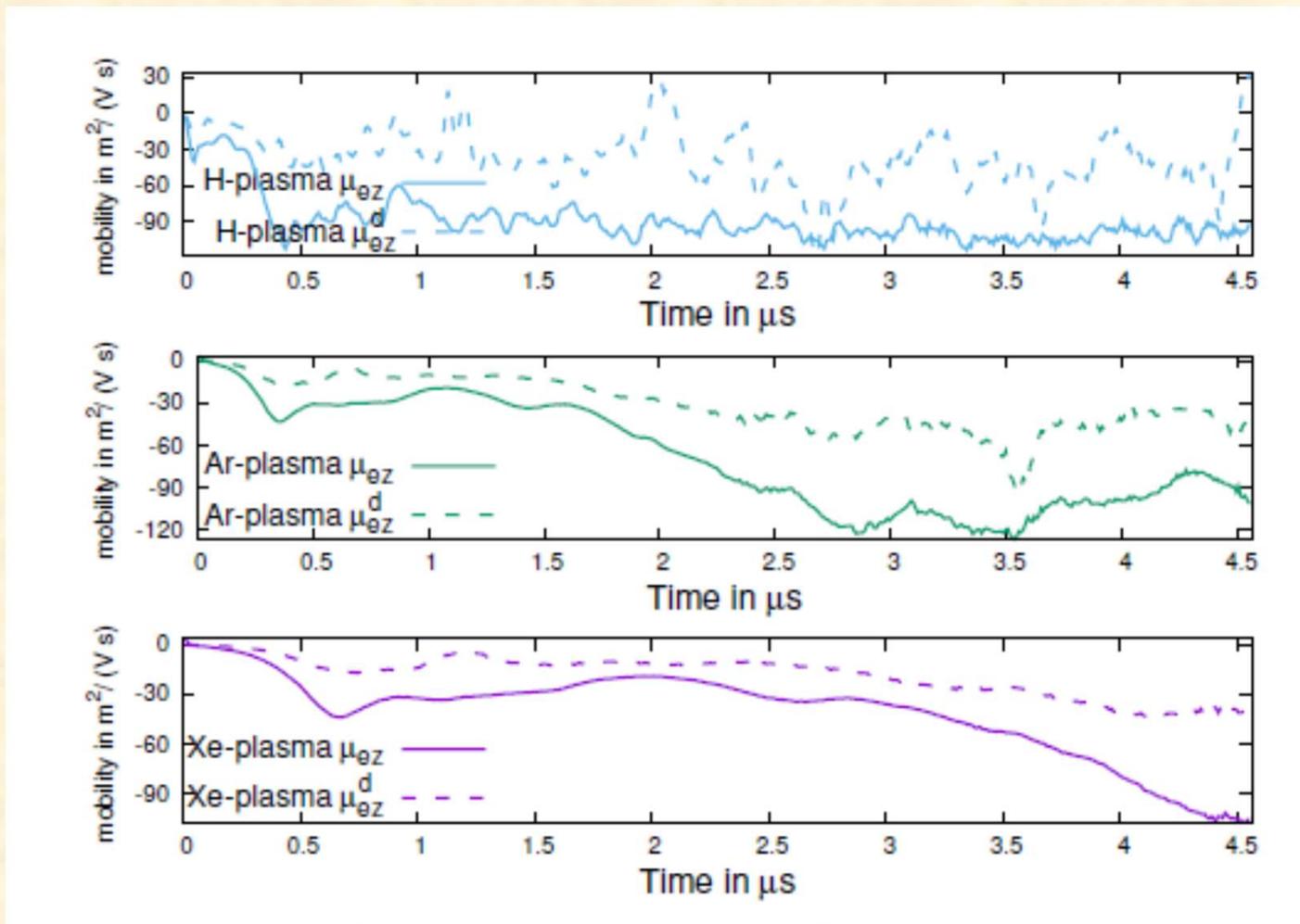
Current vortex

Mode transitions towards longer wavelengths in 2D azimuthal-radial simulations

10cmx10 cm

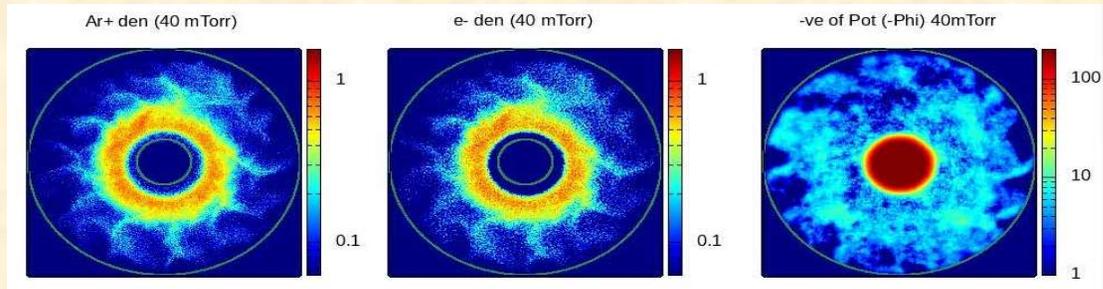


Transitions in anomalous mobility are synchronous with wavelengths transitions

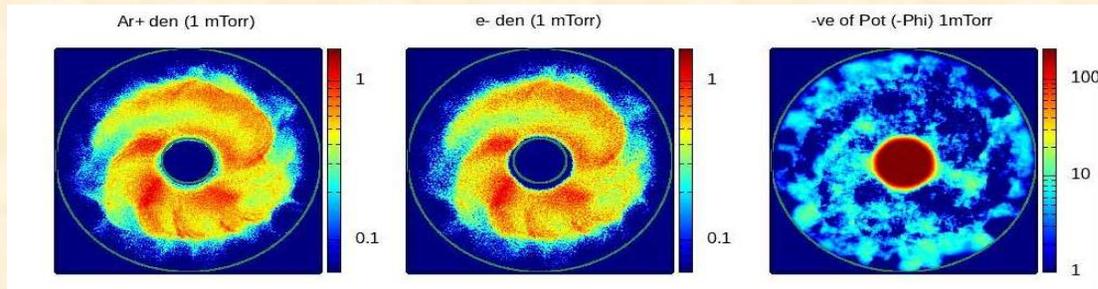


Structures modifications with neutral pressure in Penning discharge

High pressure



Low pressure



Lower pressure facilitates the development of large scale structure (spoke)

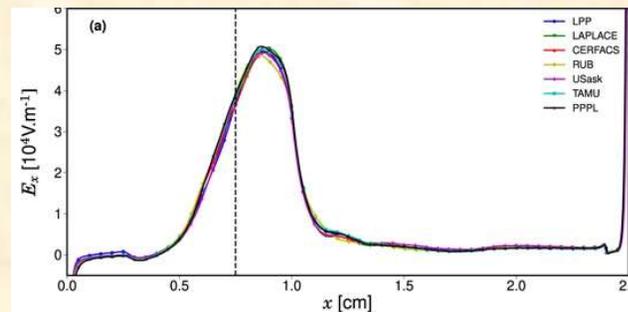
Sengupta, Smolyakov, Raitses 2021

Verification and benchmarking

ECDI structures and transport in 2D axial-azimuthal simulations:
PIC Codes benchmark, Charoy et al. PSST 2019

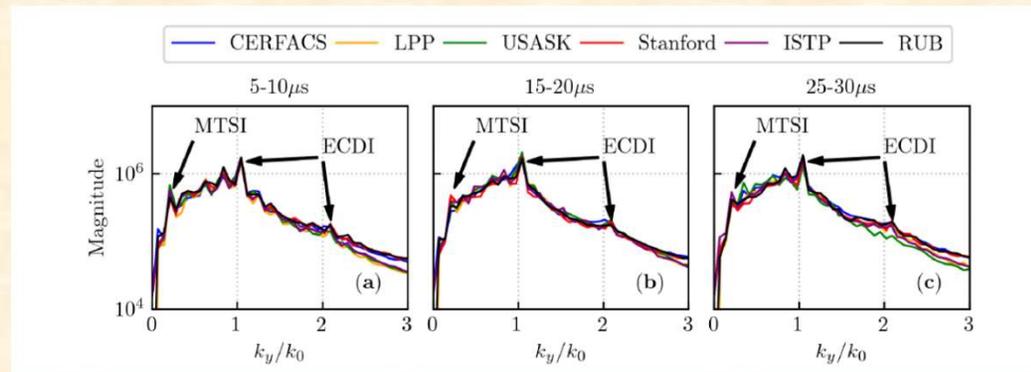
LPP, Ecole Polytechnique
LAPLACE, U Toulouse
CERFACS*
Ruhr University Bochum
U Saskatchewan
Texas AM University
PPPL, Princeton

*Centre Européen de Recherche et de Formation
Avancée en Calcul Scientifique



ECDI and MTSI in 2D radial-azimuthal simulations benchmark,
Villafana et al 2021

Fluctuations spectra

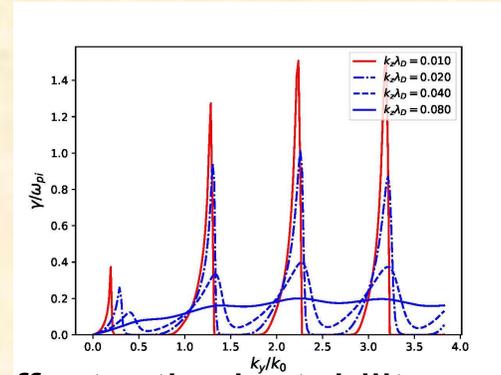


Different and independent codes, same physics and conditions

Physics issues and unsolved problems in nonlinear behavior of ECDI

Linear and nonlinear transition to the ion sound like mode?

For a finite k_z the resonance overlap due to thermal \rightarrow transition to unmagnetized ion sound instability driven by v_{ExB} beam (Gary, Sanderson 1970s)



Collisions and nonlinear broadening may provide similar effects, the instability proceeds and saturate as unmagnetized ion-sound, Lampe .., 1970 ?

Quasilinear approach, Lafleur et al, 2016-2020?

Does it occur and under what conditions? 2D and 3D effects?

Is quasilinear theory of unmagnetized ion sound applicable for ECDI?

In other words, does weak magnetic field affect ion-sound turbulence?

An old debate: [Lampe .., 1970 s- instability proceeds as an ion-sound](#)

[Forslund, Biskamp, et 1970s magnetic field is crucial for saturation and heating](#)

[How does a finite B affect anomalous resistivity?](#)

[Max Planck and LANL study, 1970s, Lindman 1985, B is important!](#)

[Direct comparison Muschietti and Lembege, JGR 2013](#)

Role of **particle noise** in PIC simulations of ECDI and associated anomalous transport?

Strong heating and absence of saturation in PIC simulations of ECDI?

Direct comparison Muschietti and Lembège, JGR 2013

Identical parameters except B : ECDI shows much stronger spectral power

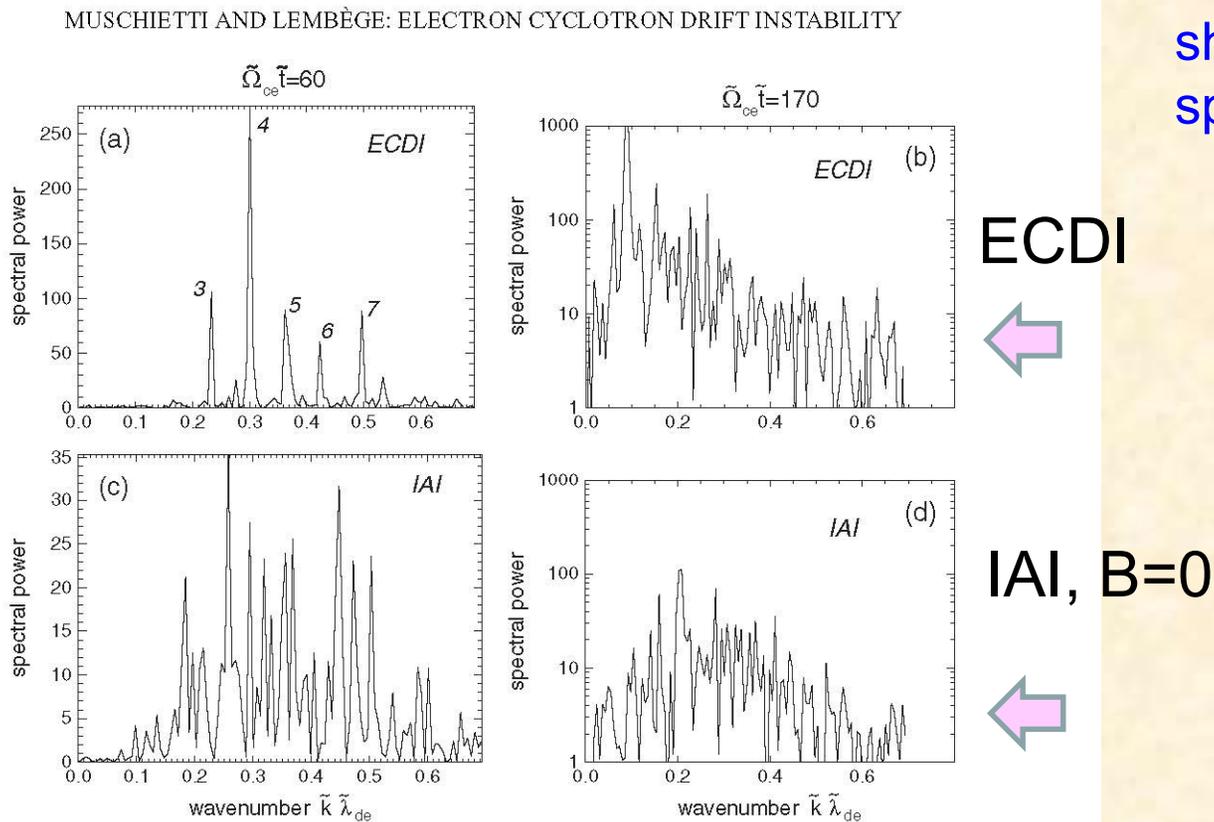


Figure 13. Snapshots of the electrostatic energy spectrum at two times, $\tilde{\Omega}_{ce} \tilde{t} = 60$ and 170, comparing two different simulation runs: (a, b) ECDI reference run with $\tilde{B}_0 = 5$ and (c, d) IAI run with $B_0 = 0$. Apart from \tilde{B}_0 , other parameters are identical (cf. Table 2).

Strong heating and absence of saturation in PIC simulations of ECDI. Universal property of existing simulations so far?

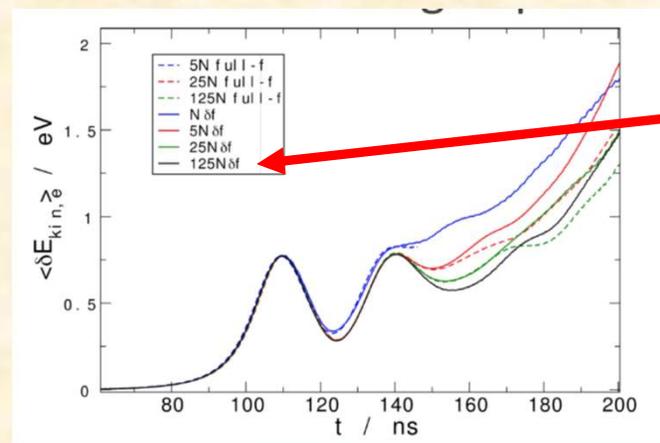
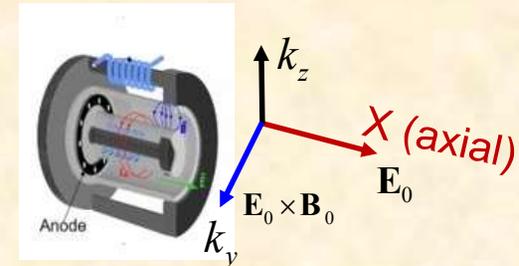
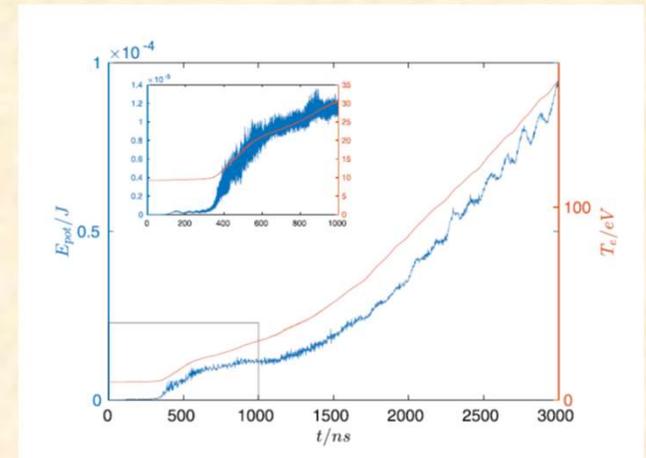
Often is “cured” with particles replacement,
 “virtual length” model- particles are refreshed
 (from cold distribution) after they travel a fixed distance

Particle replacement=effective collisions

In simulations without replacement
 Janhunen et al, PoP 2018, $T > 500$ eV
 No saturation in energy of fluctuations
 either

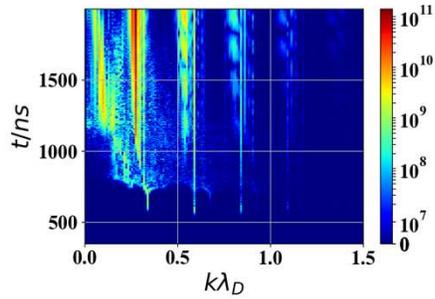
Axial transport = heating
 Spurious transport=spurious heating

Spurious particle heating and transport in full and delta-f
 PIC simulations

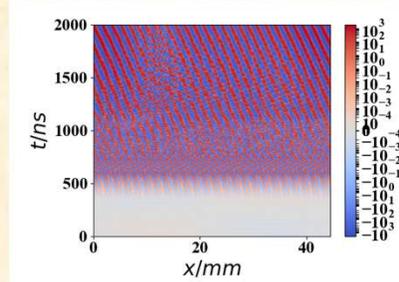


N=10 000, 1.25M
 particles per cell
 Ridiculous for
 practical simulations

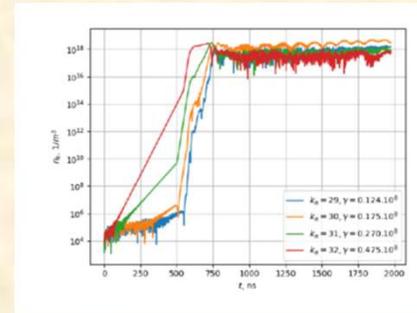
Direct Vlasov simulations of ECDI (one-dimensional)



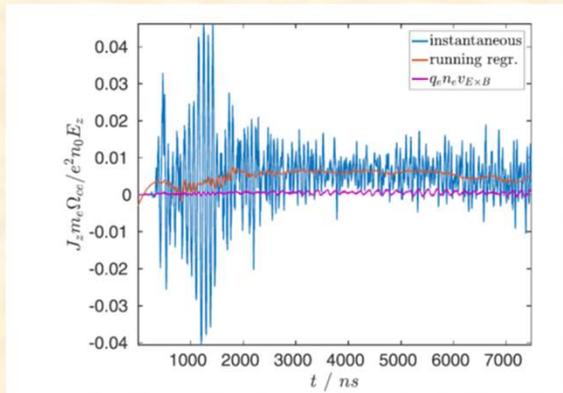
Cyclotron resonances



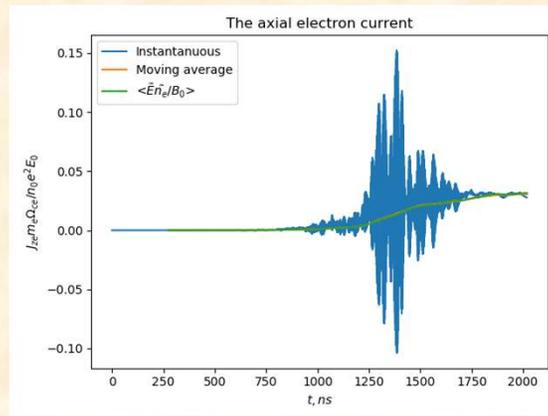
Mode transitions and inverse cascade



Energy saturation!
due to the electron trapping



PIC (no particles replacement)
Janhunen POP 2018



Vlasov

Major differences:
Energy saturates in Vlasov

$\langle \tilde{E}_\theta \tilde{n} / B \rangle$ transport is different

.....

Tavasoli, Smolyakov 2021

Particle noise effects is a difficult problem for ECDI

Discrete particle noise in particle-in-cell simulations of plasma microturbulence

Cite as: Phys. Plasmas 12, 122305 (2005); <https://doi.org/10.1063/1.2118729>

Submitted: 03 August 2005 . Accepted: 21 September 2005 . Published Online: 12 December 2005

W. M. Nevins, G. W. Hammett, A. M. Dimits, W. Dorland, and D. E. Shumaker

Jenko, 2002] and Ref. [Lin, 2004; Lin, 2004a; Lin, 2005]. However, we will demonstrate that both the late-time decay of the ETG turbulence and the steady-state heat transport observed in our PG3EQ simulations and, by inference, in the GTC simulations reported in Ref. [Lin, 2004; Lin, 2004a; Lin, 2005] are a consequence of discrete particle noise. Hence, the PG3EQ simulations reported here and the GTC simulations reported in Ref. [Lin, 2004; Lin, 2004a; Lin, 2005] have nothing to say about steady-state heat transport associated with ETG turbulence in experimental plasmas.

ETG is an electron scale ρ_e microinstability, ECDI is on a shorter scale and can be even more difficult with weak magnetic field

$$\frac{\lambda_D^2}{\rho_e^2} = \frac{\omega_{ce}^2}{\omega_{pe}^2} < 1$$



From EPOCH manual. EPOCH is another PIC code widely used in space physics community

Noise disasters in tokamak simulation.

- PIC simulations predicted lower levels of transport in tokamaks than Eulerian simulations.
- Seemed to be converged with particle number (but weren't!). (See Hammett et. al., 2006)
- It was the diffusion due to noise that killed them.
- Lessons:
 - Understand how much noise is in the system and its effect.
 - Convergence scans necessary but liable to misinterpretation.

Ben F McMillan,

Centre for Fusion, Space and Astrophysics,
Physics Department, University of Warwick, UK

Acknowledgements to the EPOCH team.

In summary

Turbulence in ExB discharges coexist at small and large scales

Experimental evidences of small scale fluctuations (and large scale) exist

Small scales are most unstable, subsequently feed large scales (inverse cascade)

Plasma and magnetic field gradients, ExB drift, and collisions are the drives.

Respectively: gradient-drift, lower hybrid instabilities, ECDI, ion-sound. First principle anomalous transport has been demonstrated in reduced fluid model simulations.

Relative importance of the driving factors varies between different regions (near-anode, acceleration zone, plume and near-cathode), mutual coupling in realistic conditions is still unclear

ECDI/EDI: Relatively easy to obtain in PIC numerical codes, many groups...

Has been well demonstrated in 1D (azimuthal) and 2D (azimuthal-axial, azimuthal-radial) simulations, 3D are rare and not conclusive but needed

Role of gradients and mutual coupling?

PIC noise effects on transport and heating? Saturation mechanisms?

Conversion of simulation results into practical predictions is still difficult.

Coordinated efforts: codes testing and benchmarking; suite of test cases based on analytical insights, codes verification metrics, codes validation (agreement with experiment) metrics

Development of experimental diagnostics and test bed experimental devices

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University of Saskatchewan, Saskatoon SK, Canada

Y. Raitses, I. Kaganovich, PPPL, Princeton USA

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Compute Canada

There is more on ExB plasma physics, eg, plasma-material Interactions, magnetic nozzle acceleration, .. see

Physics of $E \times B$ discharges relevant to plasma propulsion and similar technologies

F

Cite as: Phys. Plasmas **27**, 120601 (2020); <https://doi.org/10.1063/5.0010135>

Submitted: 07 April 2020 . Accepted: 28 July 2020 . Published Online: 16 December 2020

 Igor D. Kaganovich,  Andrei Smolyakov,  Yevgeny Raitses,  Eduardo Ahedo,  Ioannis G. Mikellides,  Benjamin Jorns, Francesco Taccogna,  Renaud Gueroult,  Sedina Tsikata,  Anne Bourdon,  Jean-Pierre Boeuf, Michael Keidar, Andrew Tasman Powis,  Mario Merino,  Mark Cappelli,  Kentaro Hara, Johan A. Carlsson,  Nathaniel J. Fisch,  Pascal Chabert,  Irina Schweigert, Trevor Lafleur,  Konstantin Matyash, Alexander V. Khrabrov, Rod W. Boswell, and  Amnon Fruchtman

COLLECTIONS

 This paper was selected as Featured

**We know many elements of complex physics of ExB plasma.
Integration is still difficult**



I think the next century will be the
century of complexity.

— *Stephen Hawking* —

I think the next [21st] century will be the century of complexity. We have already discovered the basic laws that govern matter and understand all the normal situations. We don't know how the laws fit together, and what happens under extreme conditions. But I expect we will find a complete unified theory sometime this century. There is no limit to the complexity that we can build using those basic laws.

Stephen Hawking


www.idlehearts.com

Thank you for your attention!